

Deep Learning (1470)

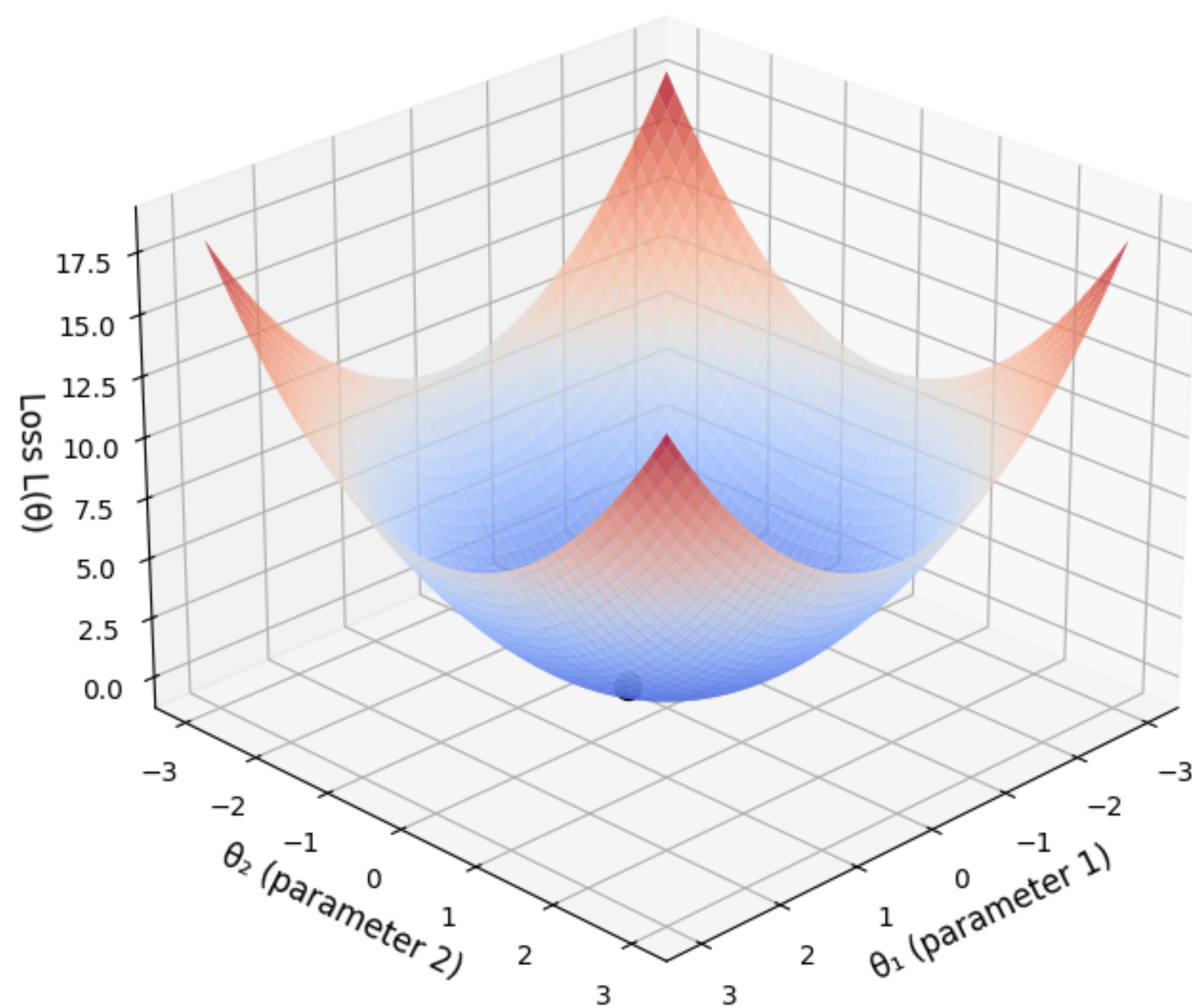
Randall Balestriero

Class 4

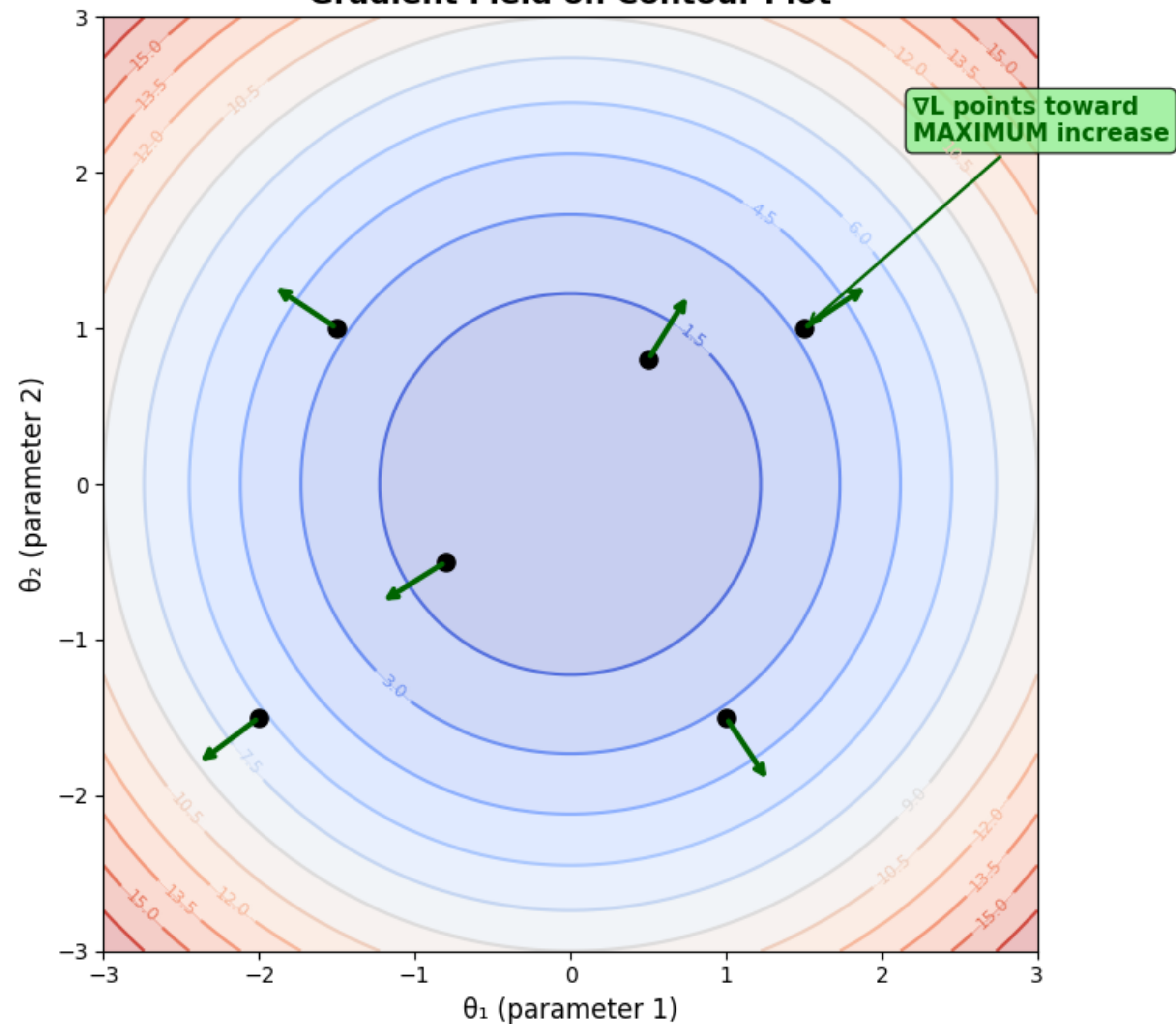
Rewind!

Gradient: Intuition

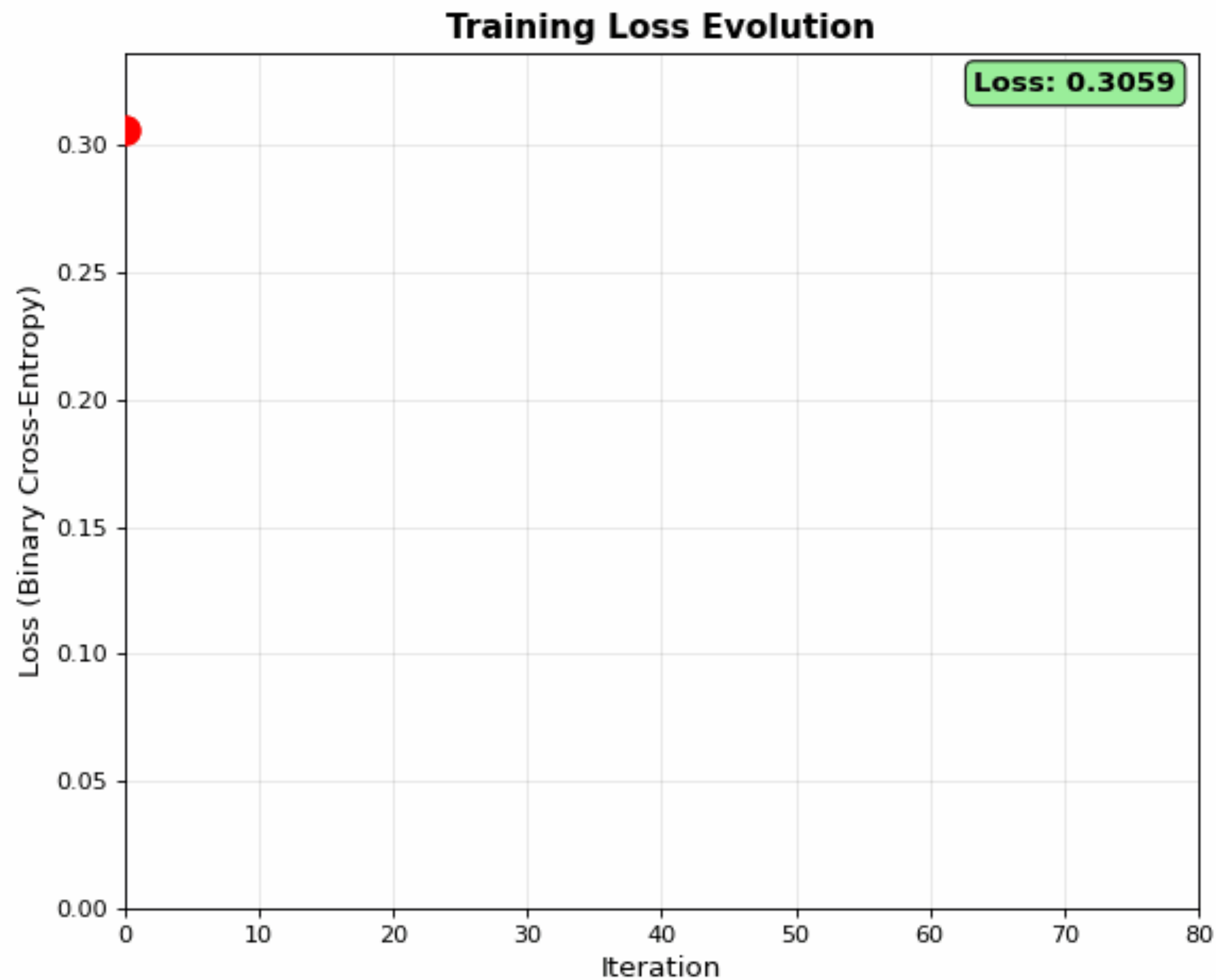
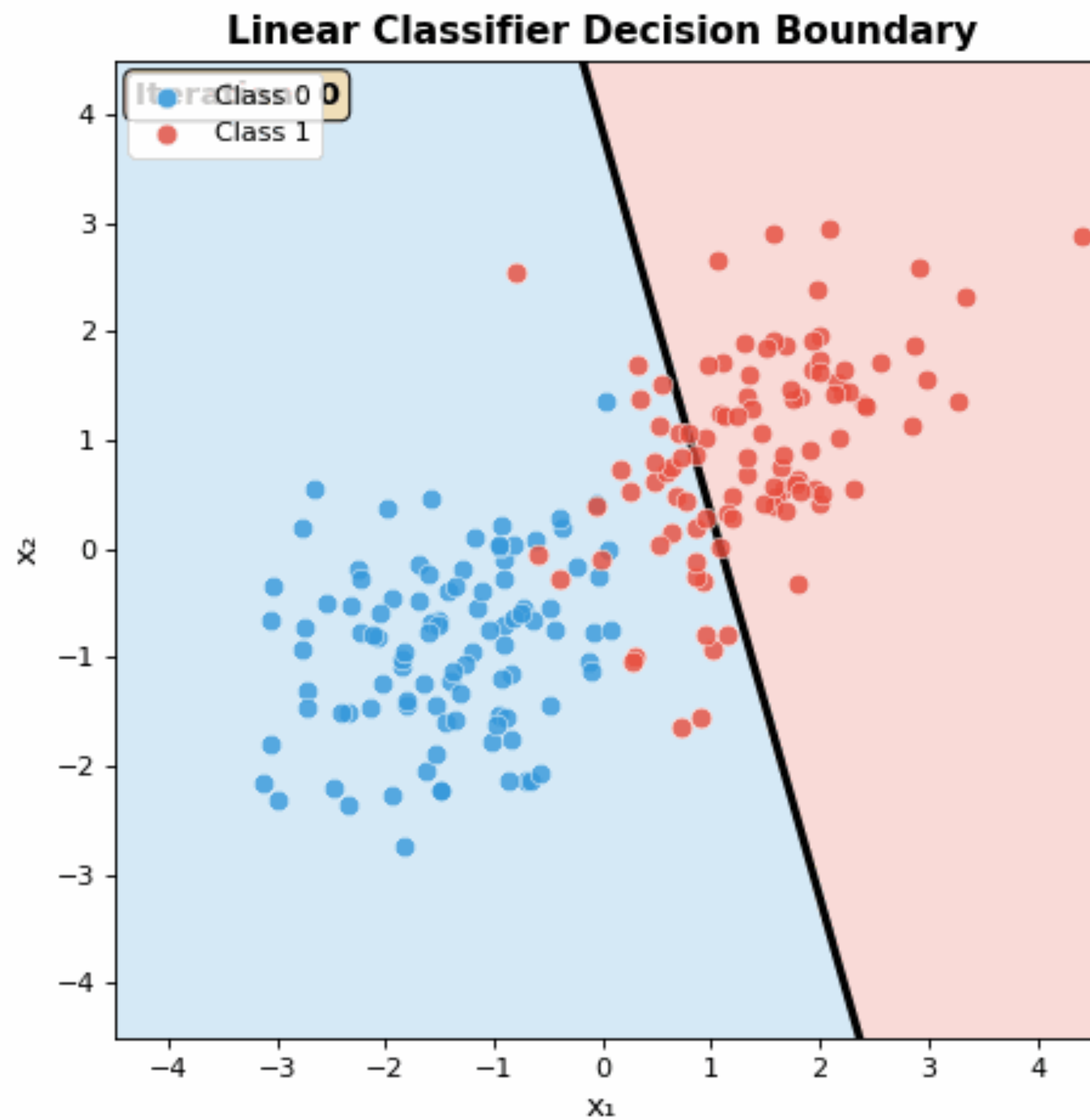
3D Loss Surface



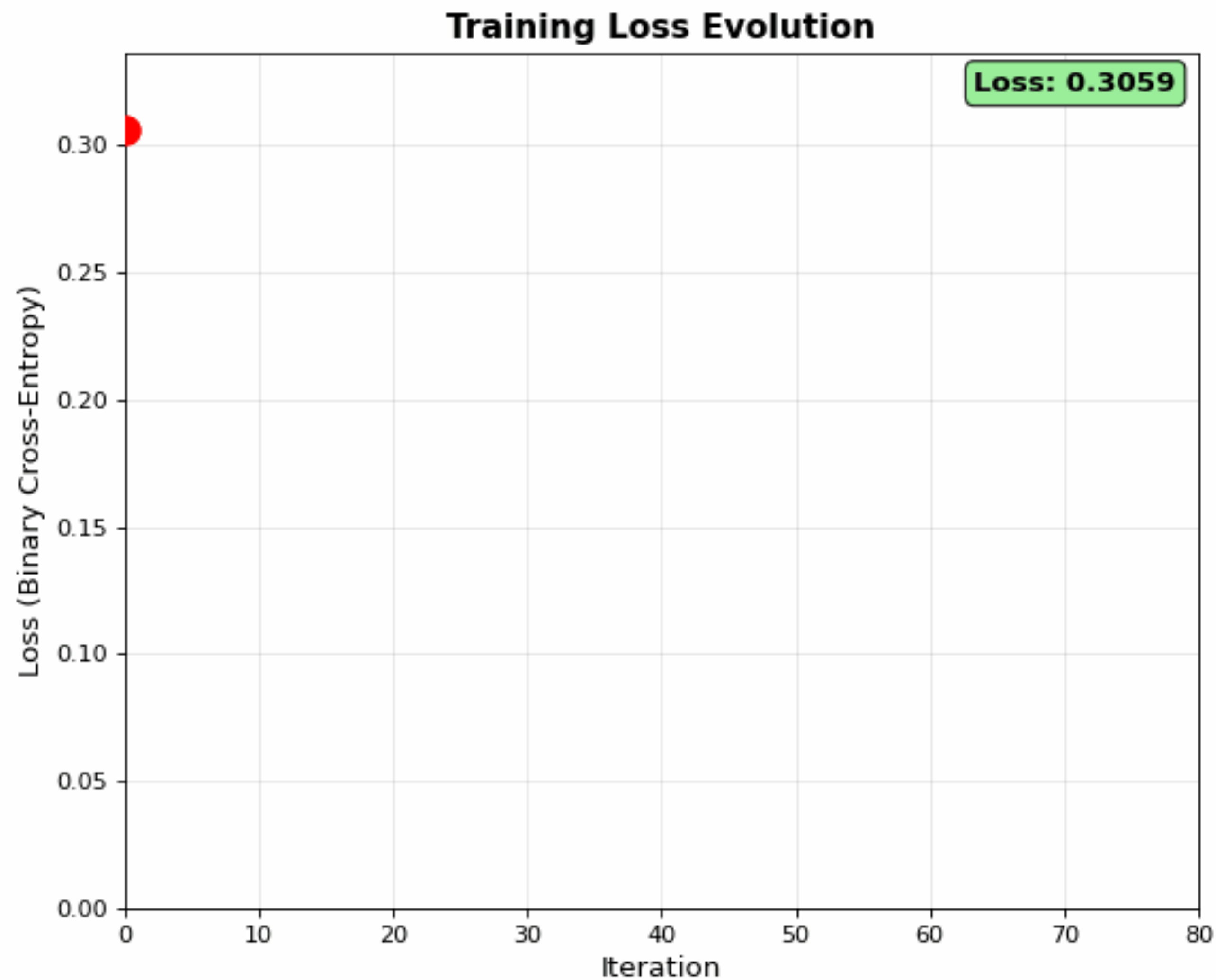
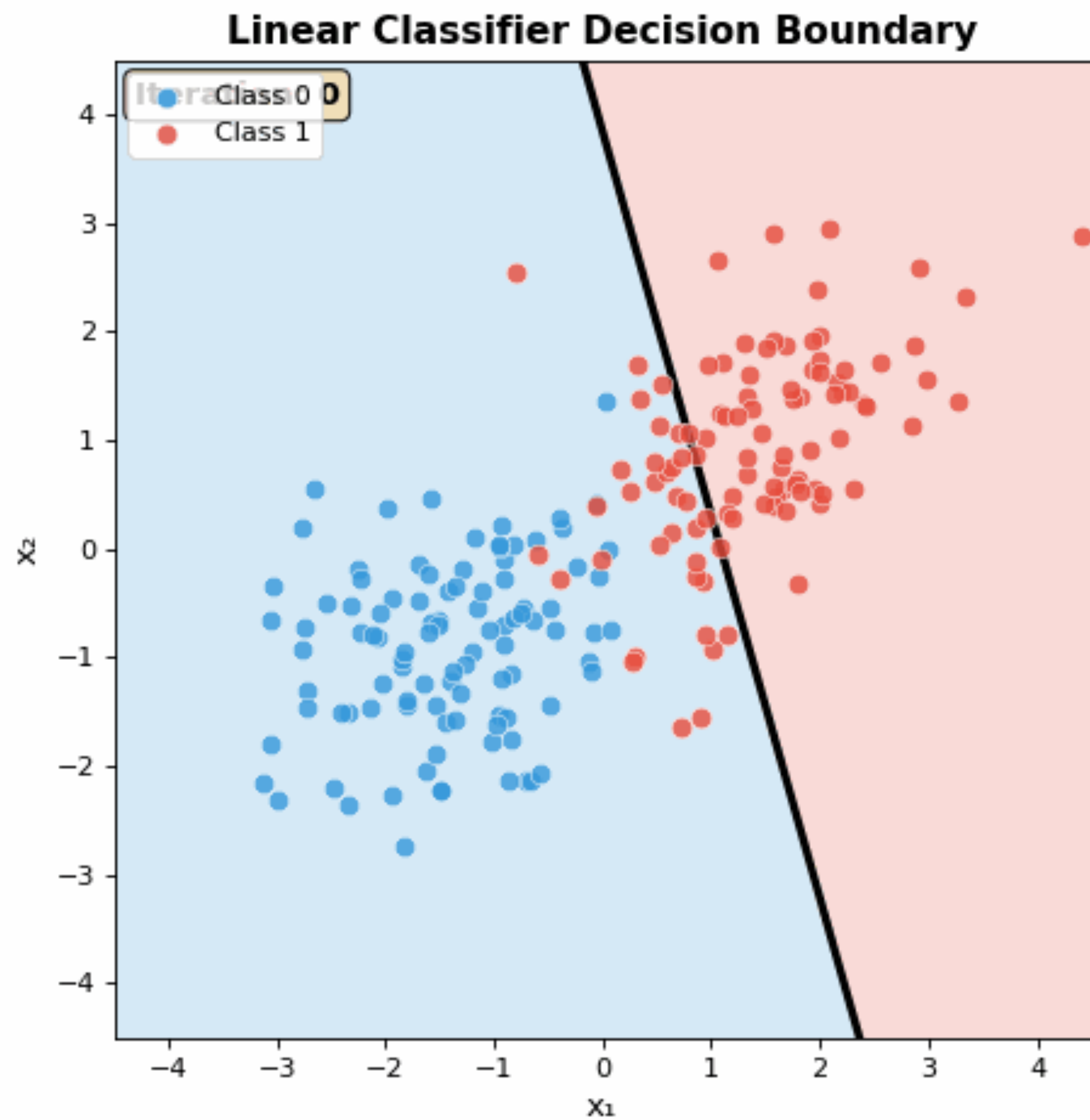
Gradient Field on Contour Plot



Gradient: Intuition



Gradient: Intuition



MNIST

The most famous dataset in Deep Learning

Modified **N**ational Institute of **S**tandards and **T**echnology database

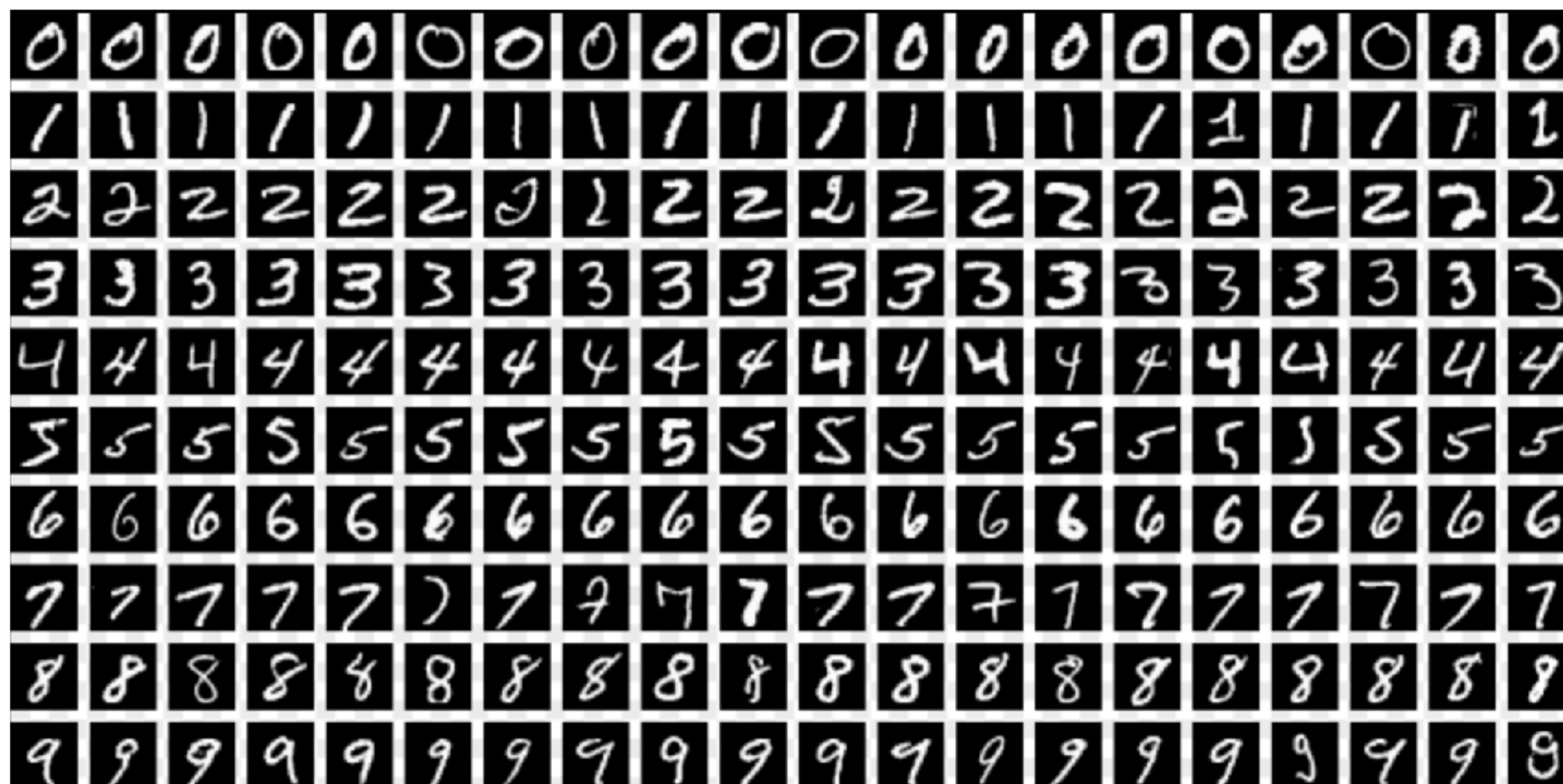


Image courtesy of Wikipedia

MNIST

MNIST

- What is D (dimension) of the samples?

MNIST

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- How many classes do we have?

MNIST

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- Do you think the classes are linearly separable?

MNIST

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- How many classes do we have?
- Do you think the classes are linearly separable?

A linear model reaches 94% accuracy!

Your First Deep Network!

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- Why do we want to use a Deep Network?

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- Could you think of “features” to extract by-hand that would improve linear model accuracy?

Your First Deep Network!

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- Could you think of “features” to extract by-hand that would improve linear model accuracy?
- Which accuracy do you think we can reach?

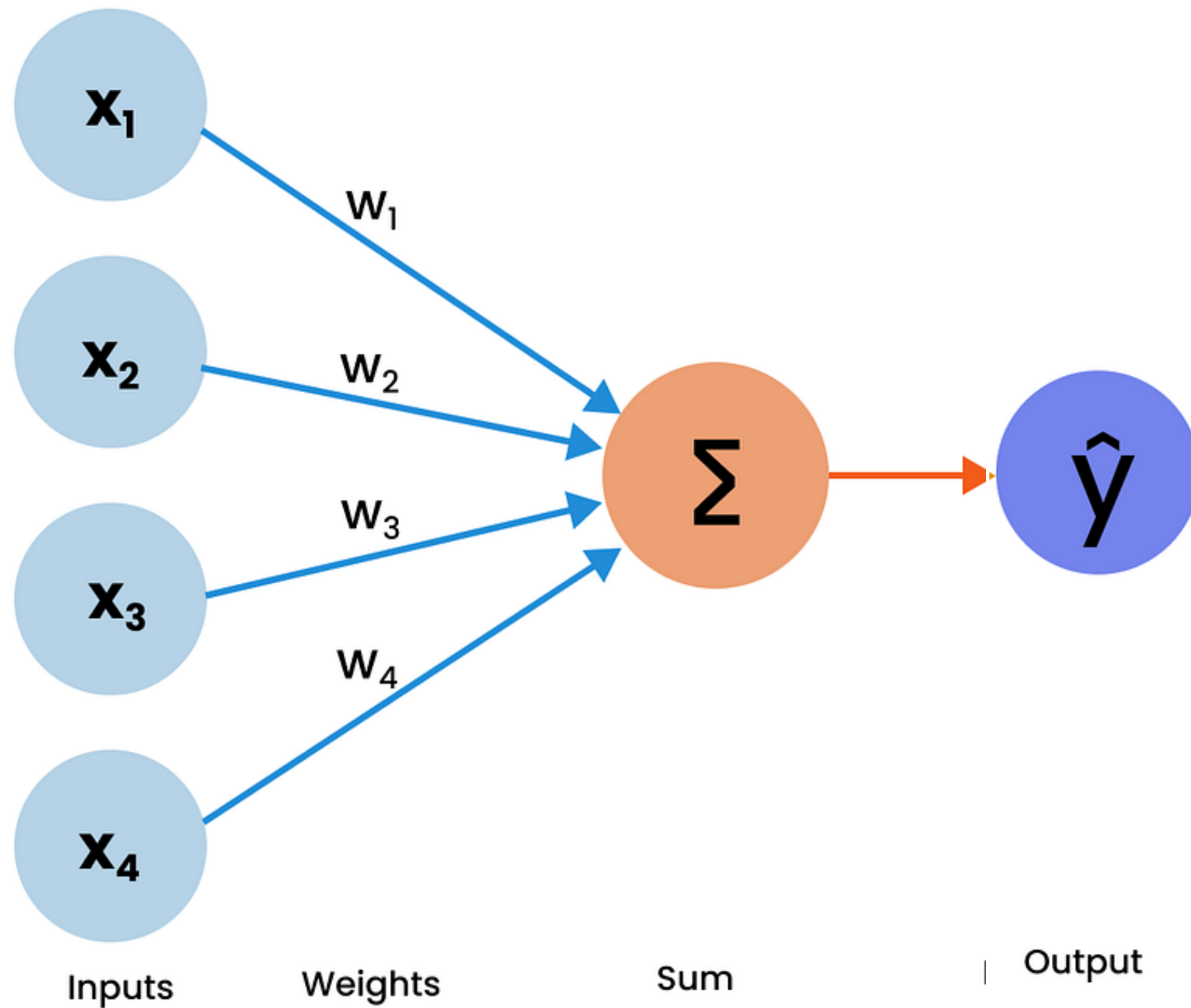
Your First Deep Network!

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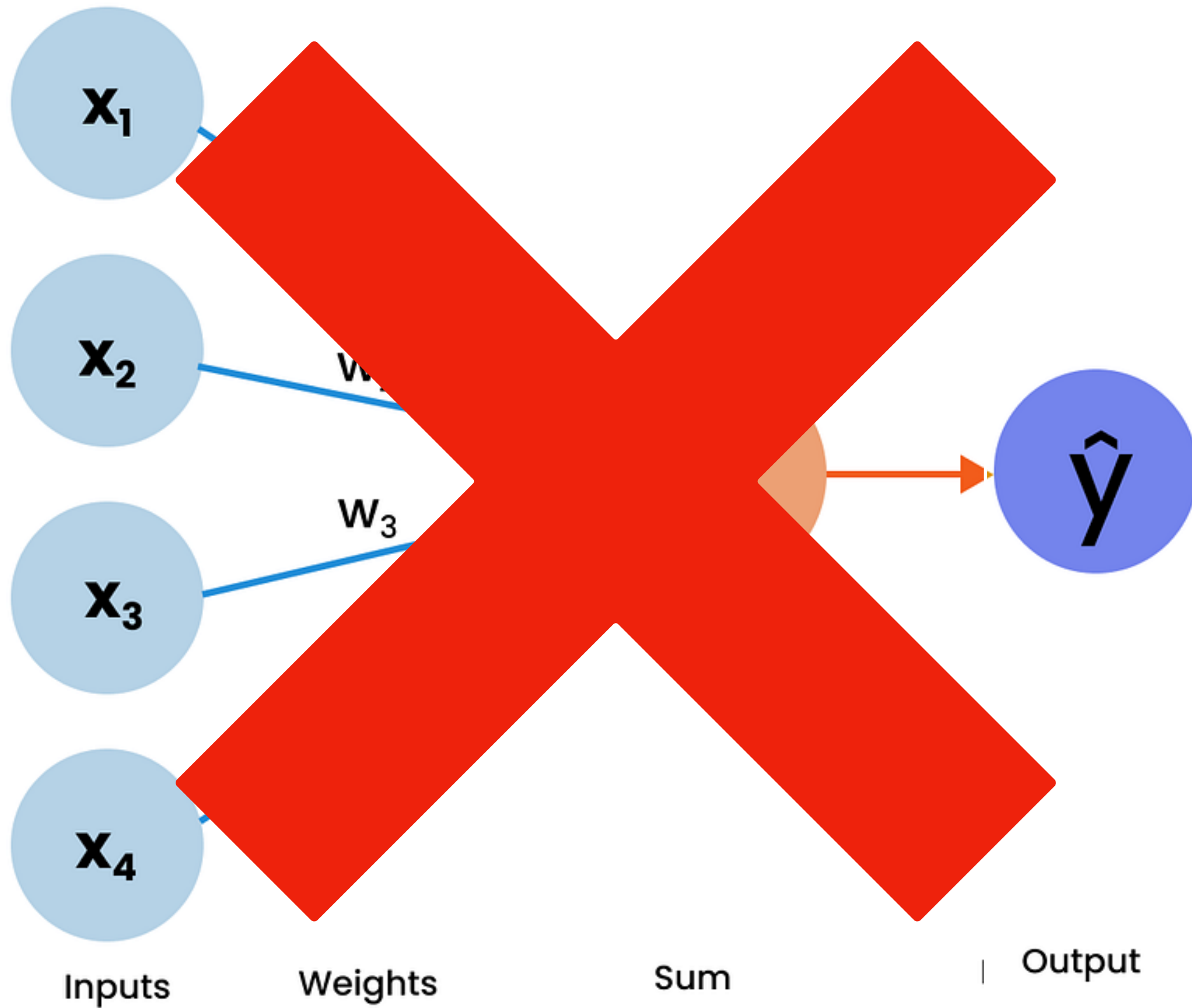
A Deep Network reaches 99.5% accuracy!

Your First Deep Network!

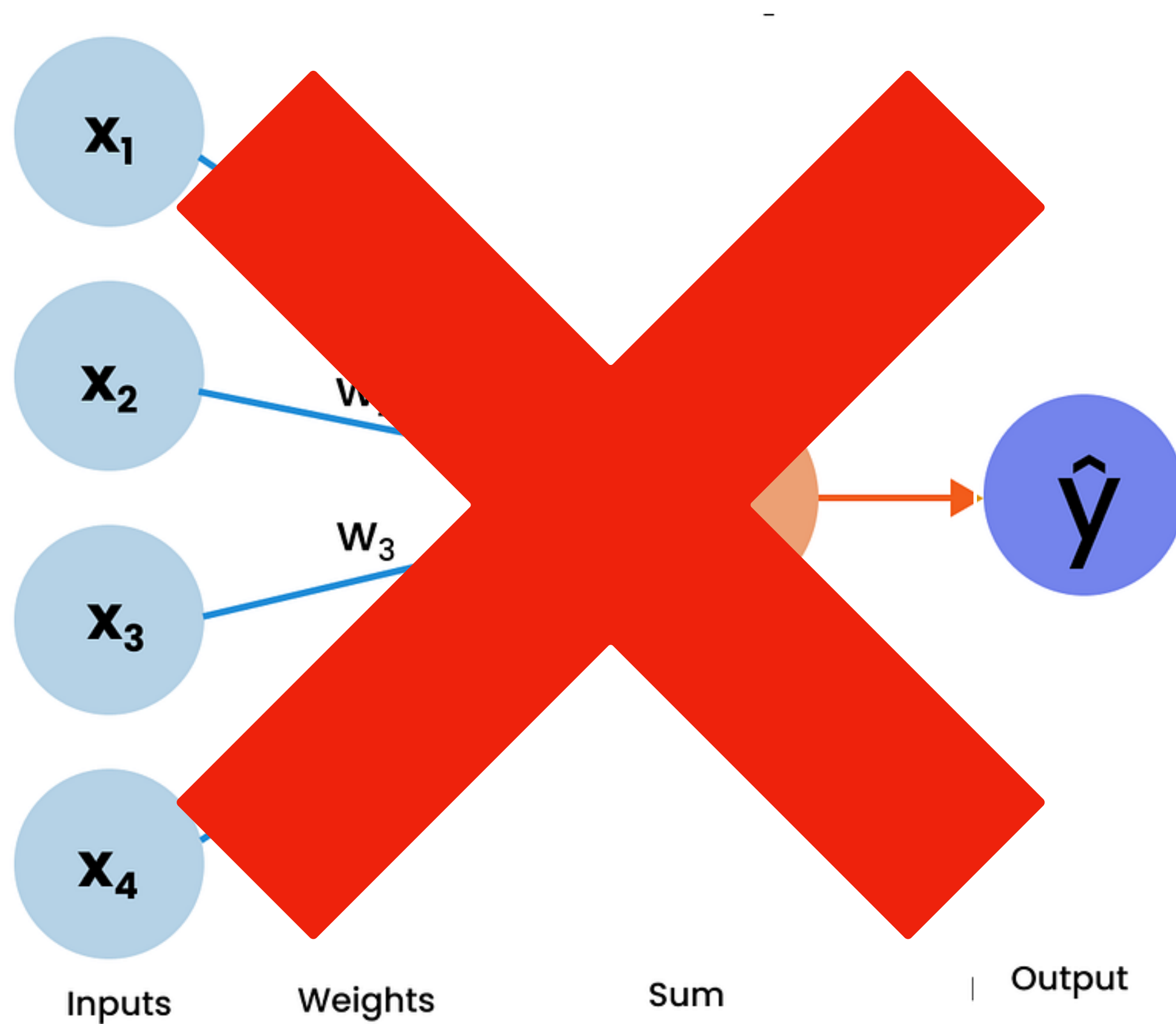
Your First Deep Network!



Your First Deep Network!

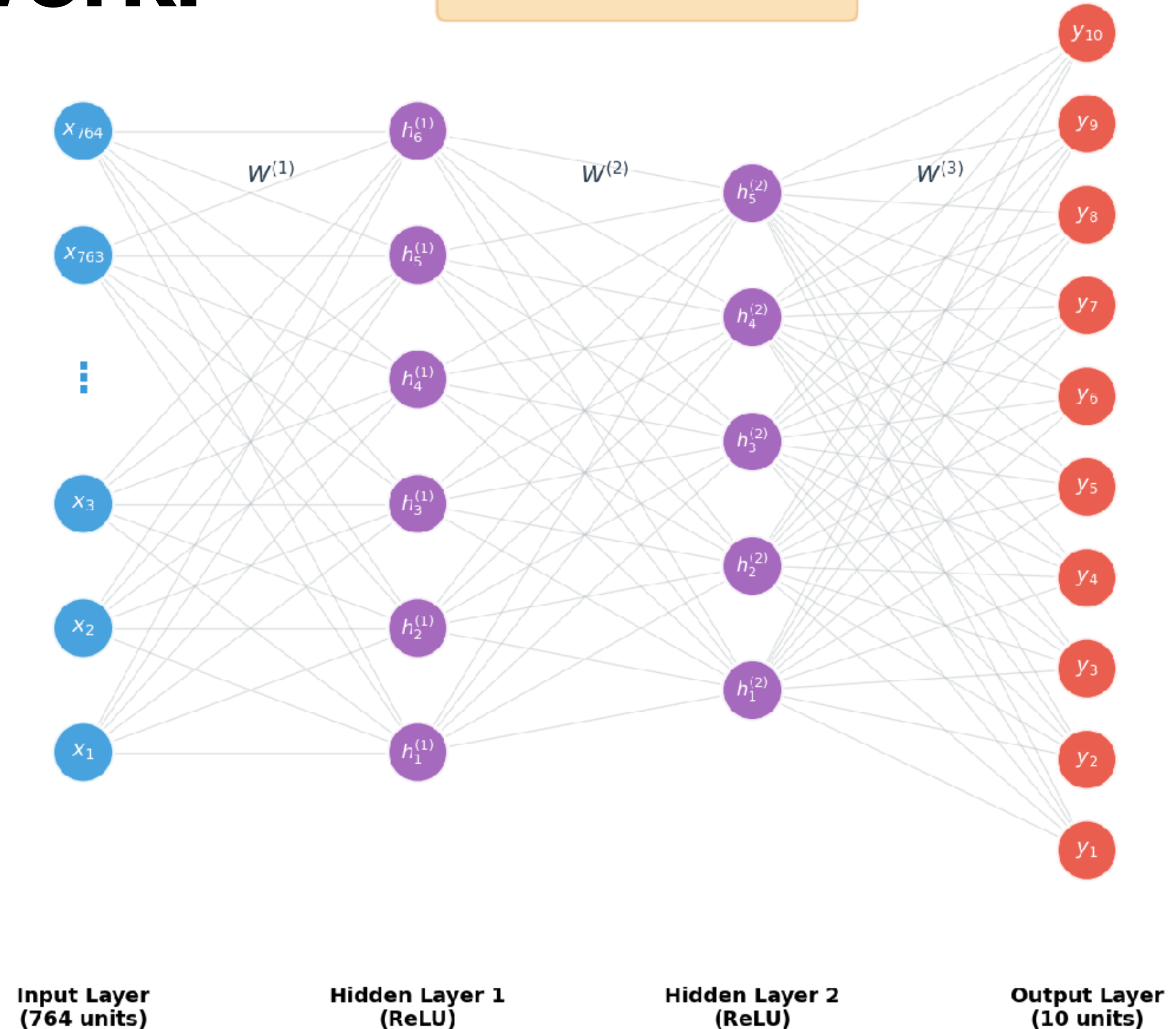


Your First Deep Network!



3-Layer MLP with ReLU Activations

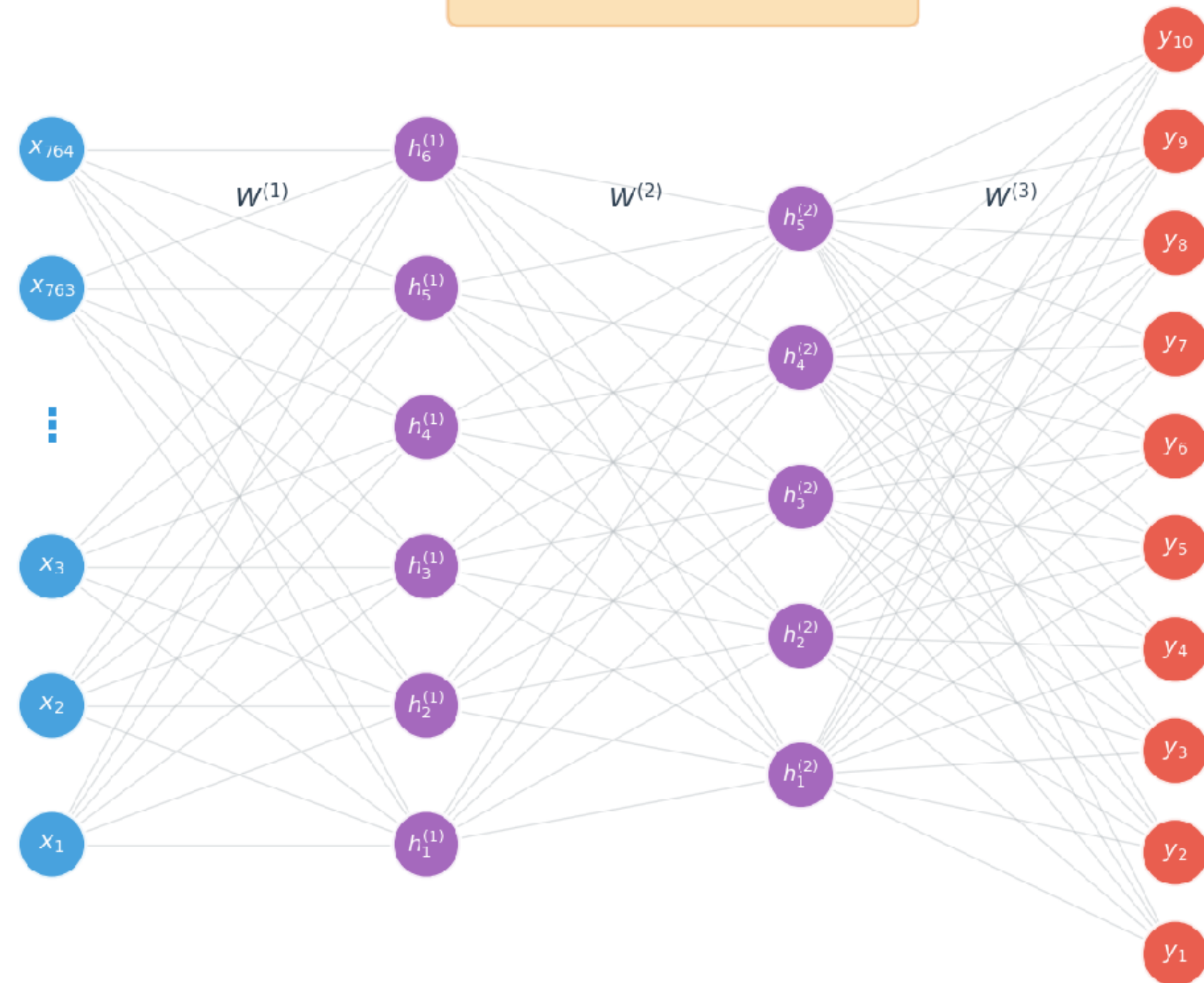
$$\text{ReLU}(z) = \max(0, z)$$



Your First Deep Network: Why?

3-Layer MLP with ReLU Activations

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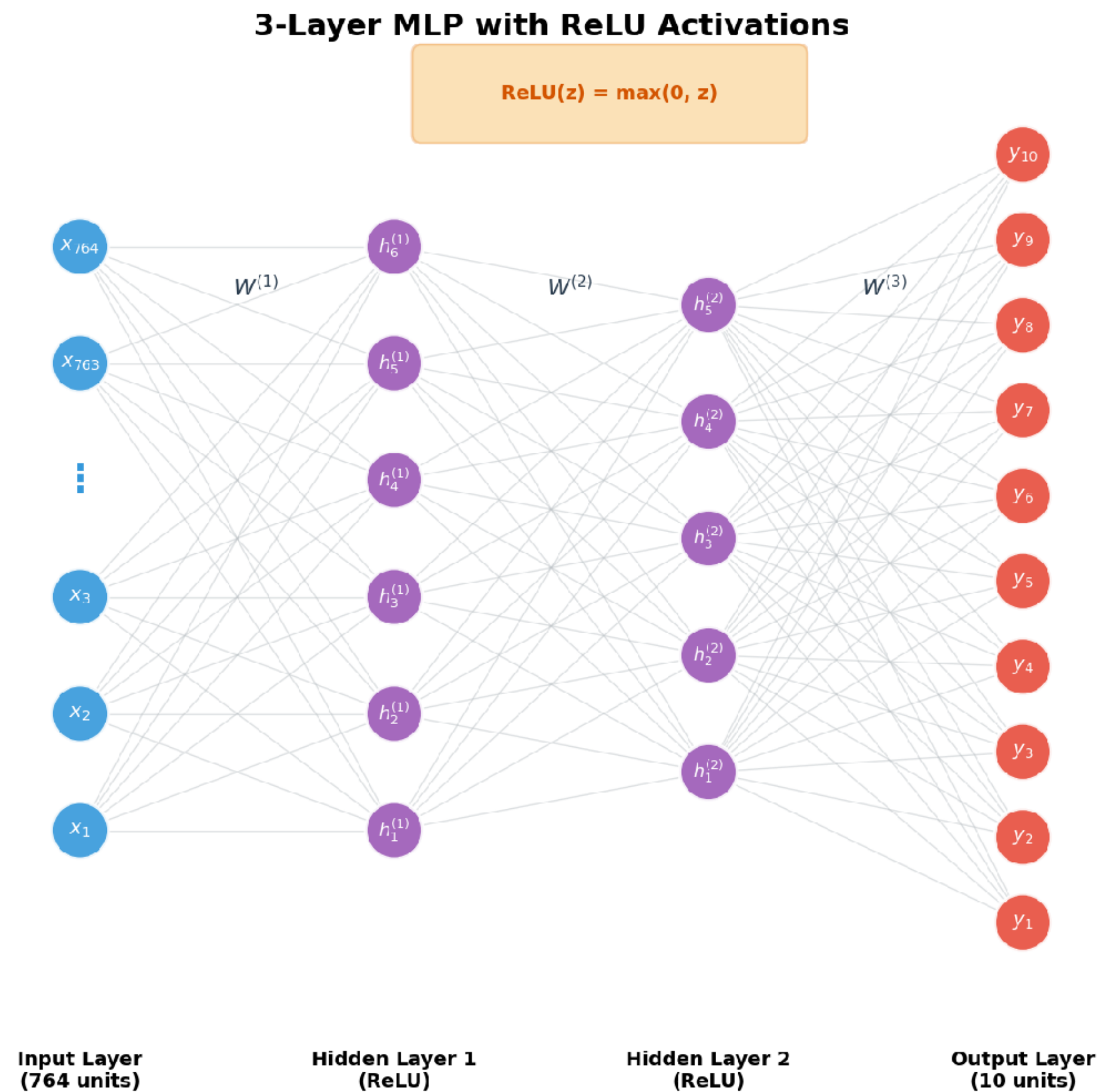
Input Layer
(764 units)

Hidden Layer 1
(ReLU)

Hidden Layer 2
(ReLU)

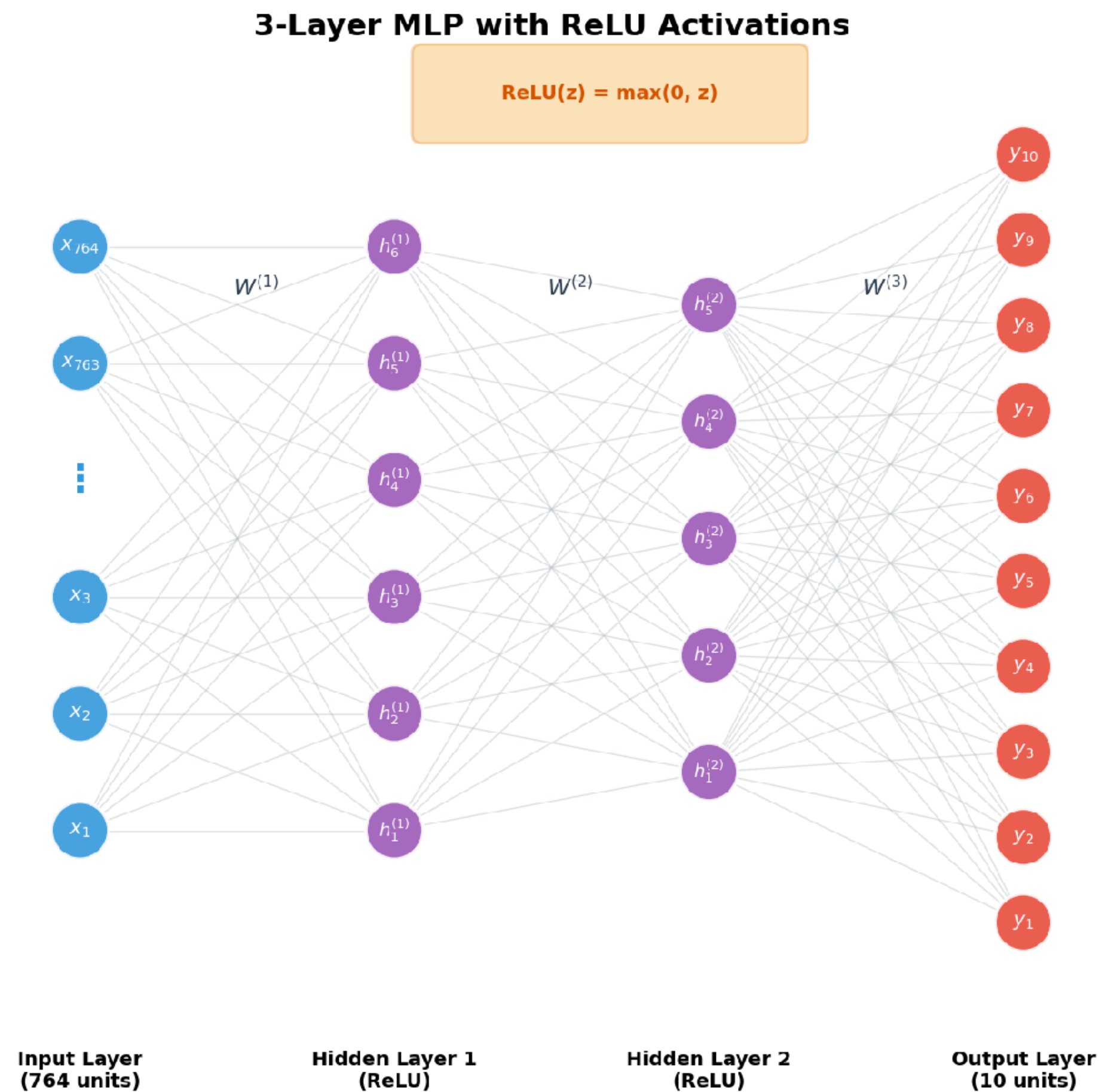
Output Layer
(10 units)

Your First Deep Network: Why?



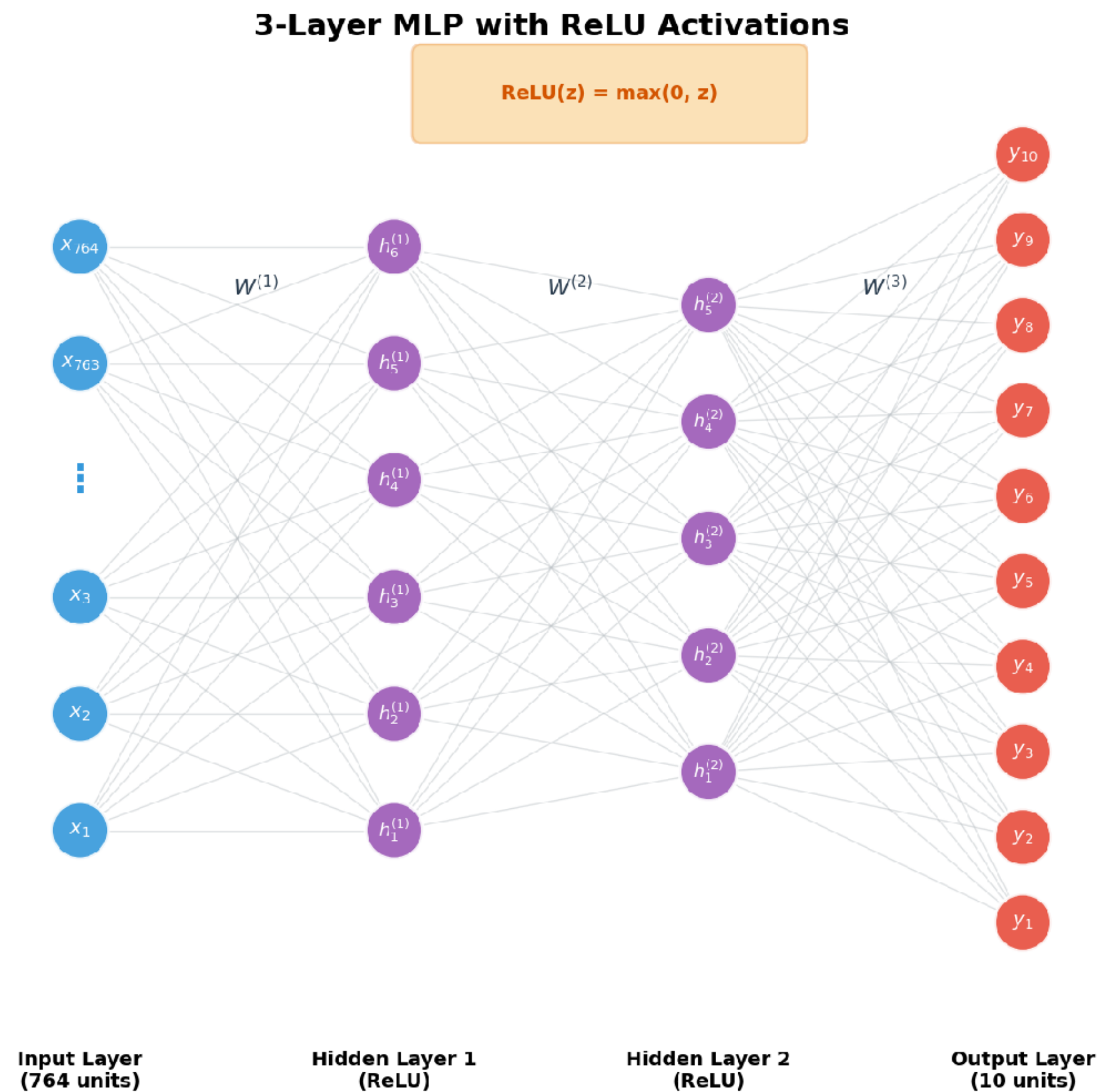
- Why 2 hidden layers?

Your First Deep Network: Why?



- Why 2 hidden layers?
- Why do we need a “ReLU”?

Your First Deep Network: Why?

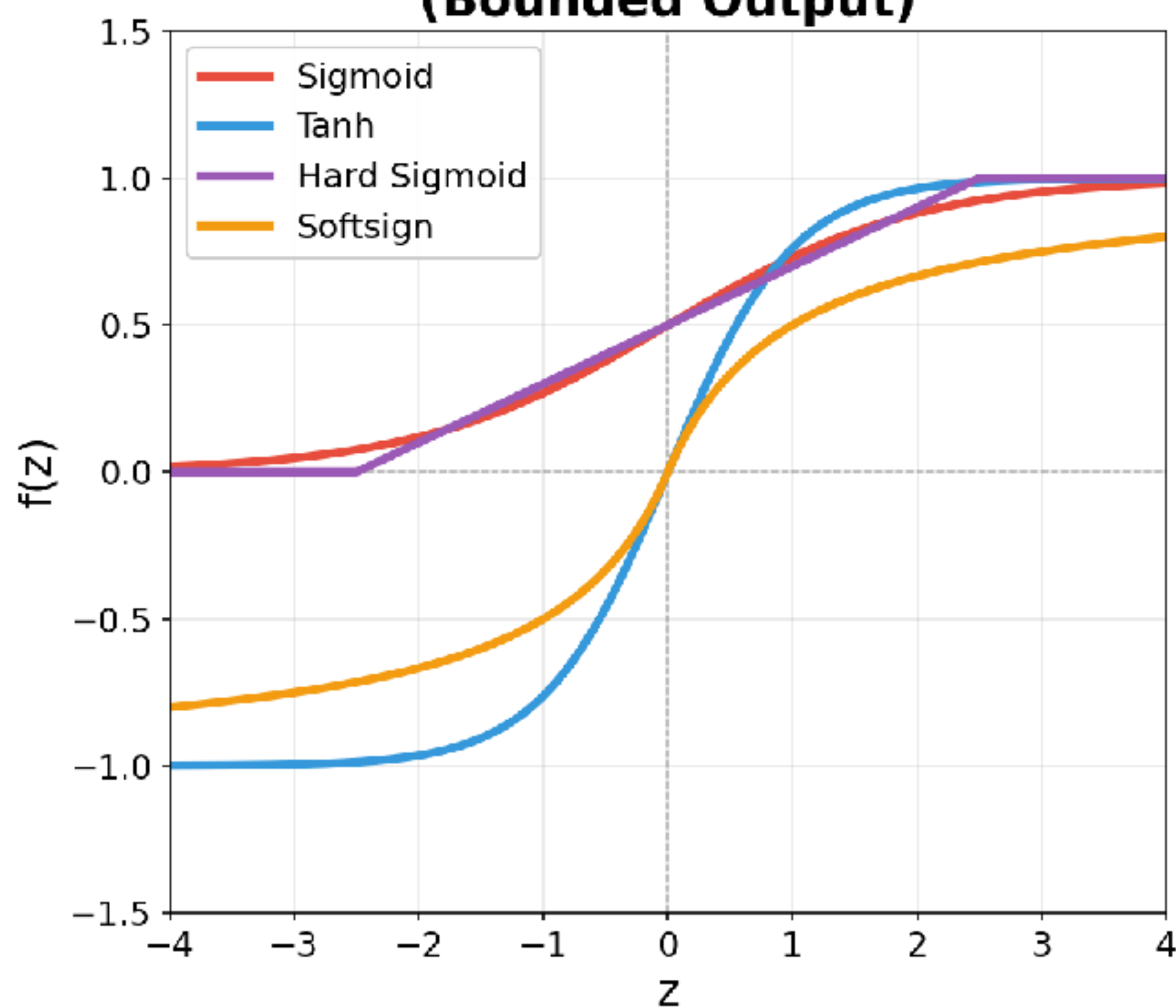


- Why 2 hidden layers?
- Why do we need a “ReLU”?
- What else besides a “ReLU”?

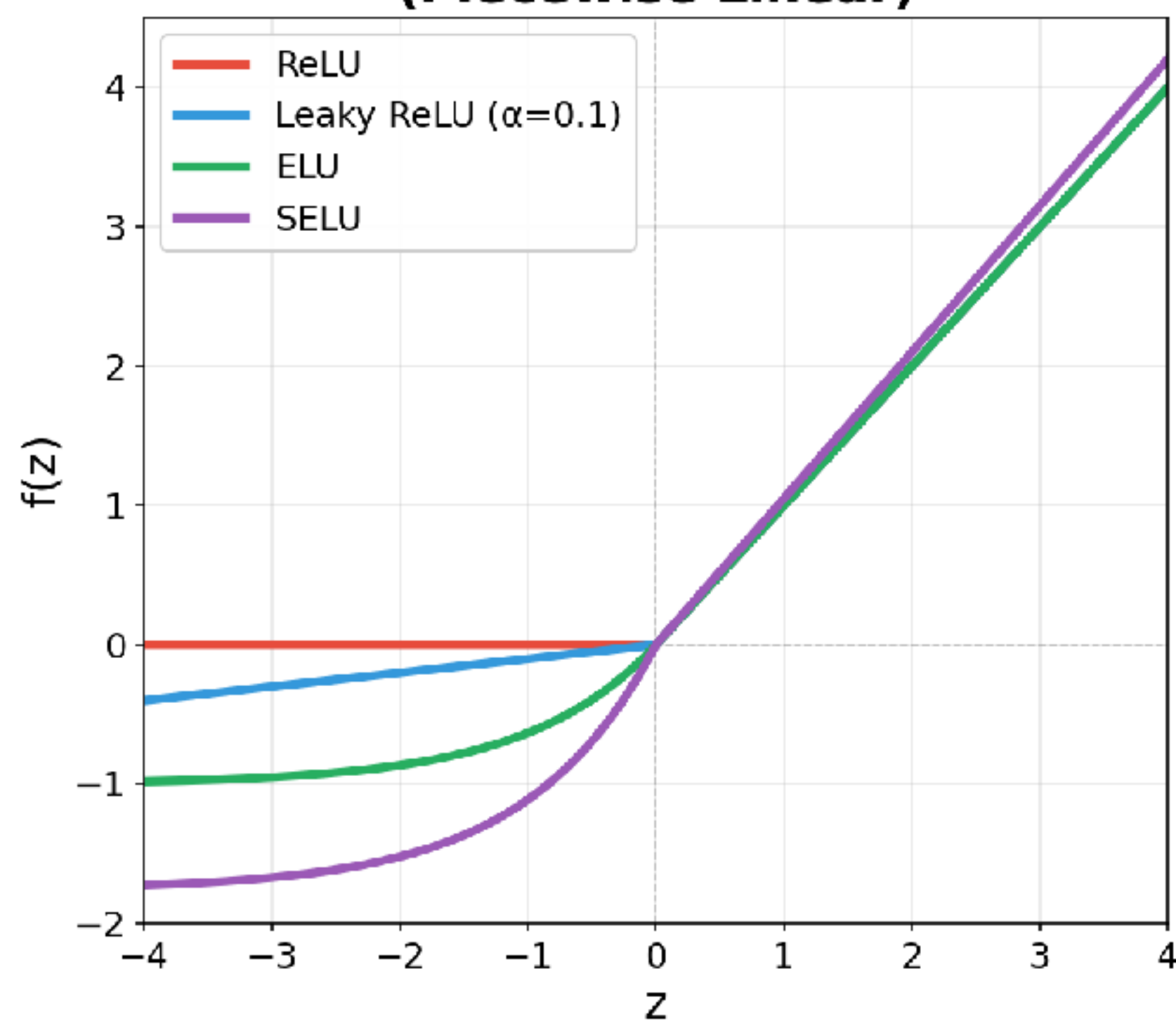
Your First Deep Network: Why?

Common Activation Functions in Neural Networks

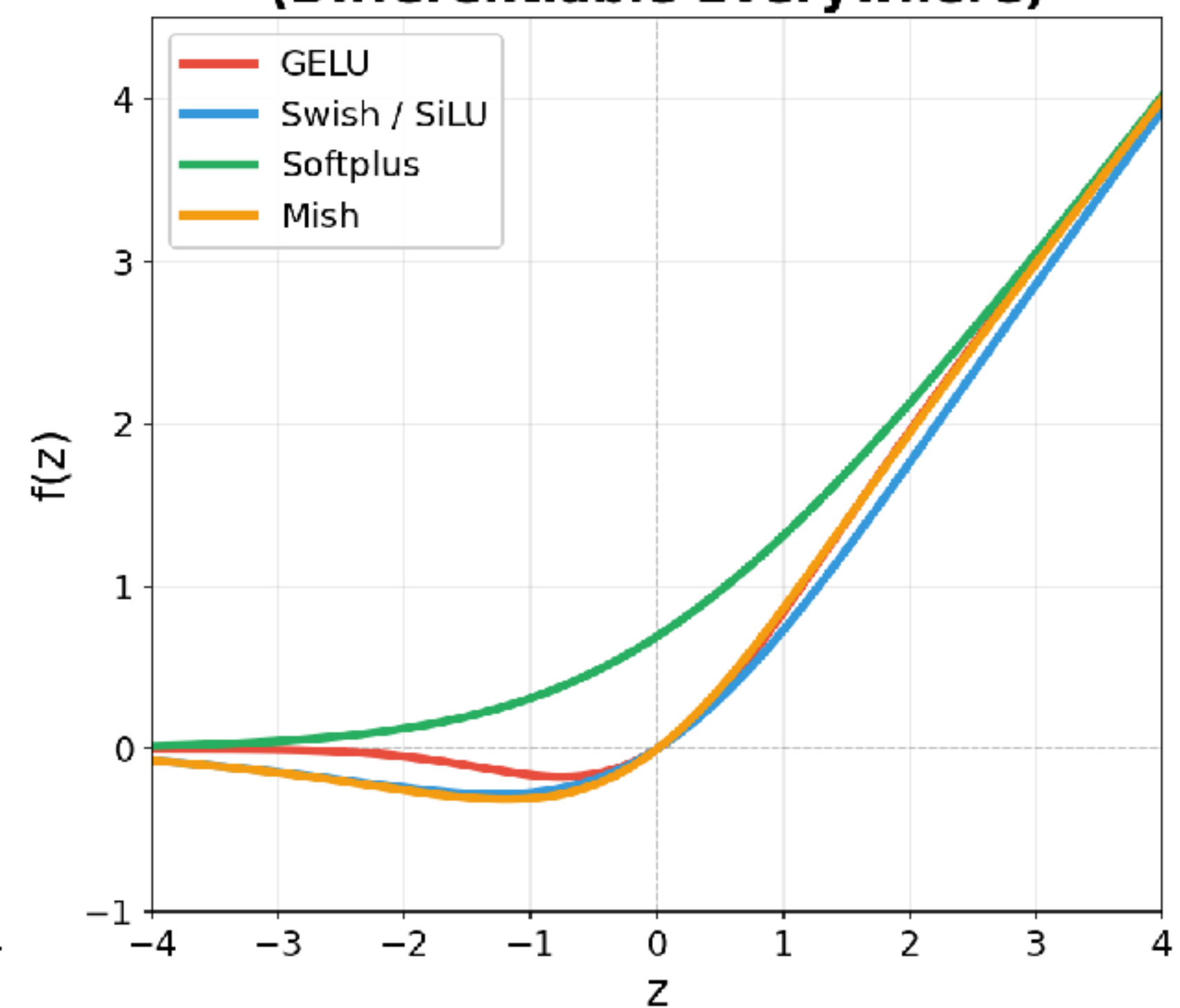
**Sigmoid-like
(Bounded Output)**



**ReLU Family
(Piecewise Linear)**



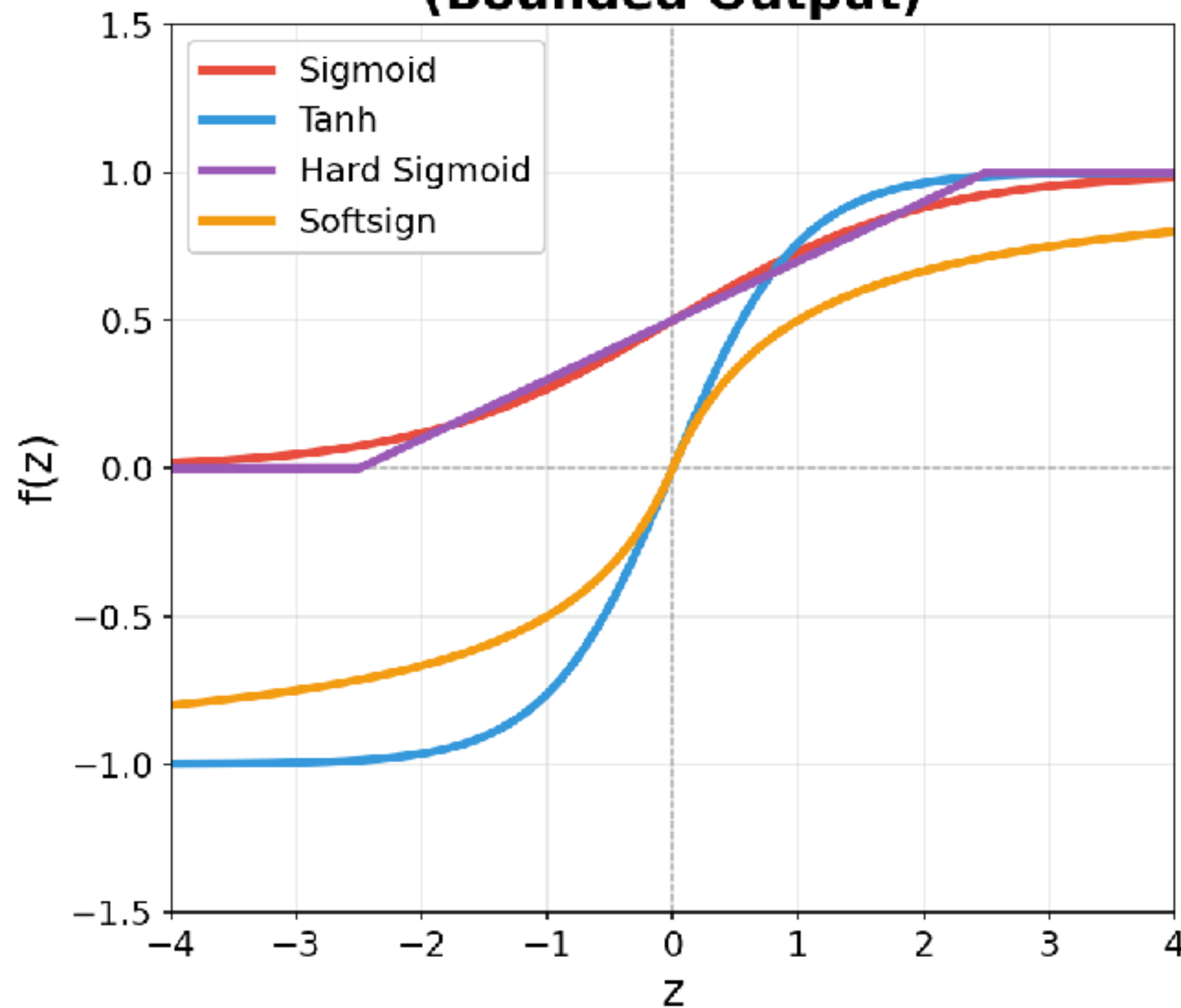
**Smooth Modern
(Differentiable Everywhere)**



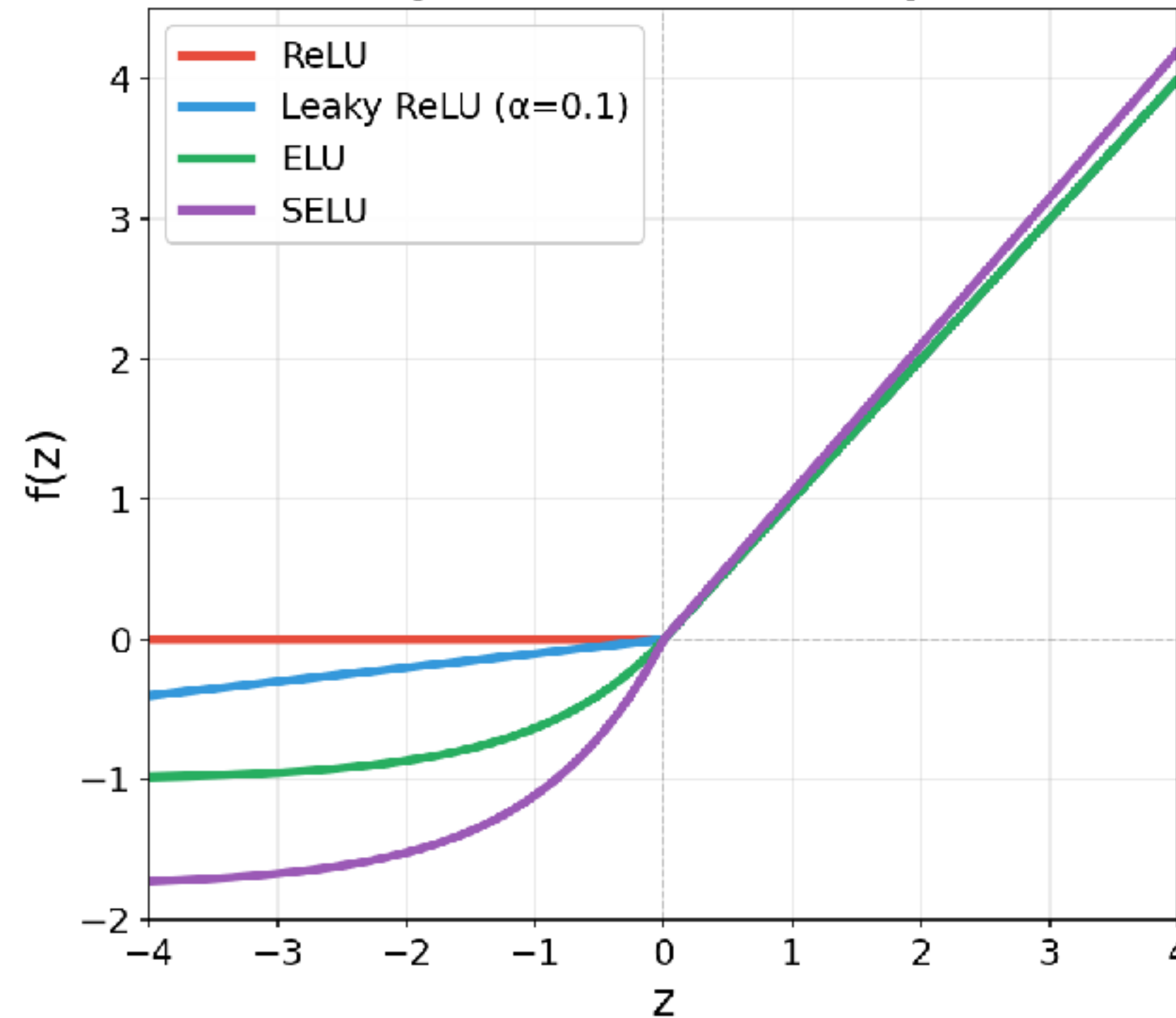
Your First Deep Network: Why?

Common Activation Functions in Neural Networks

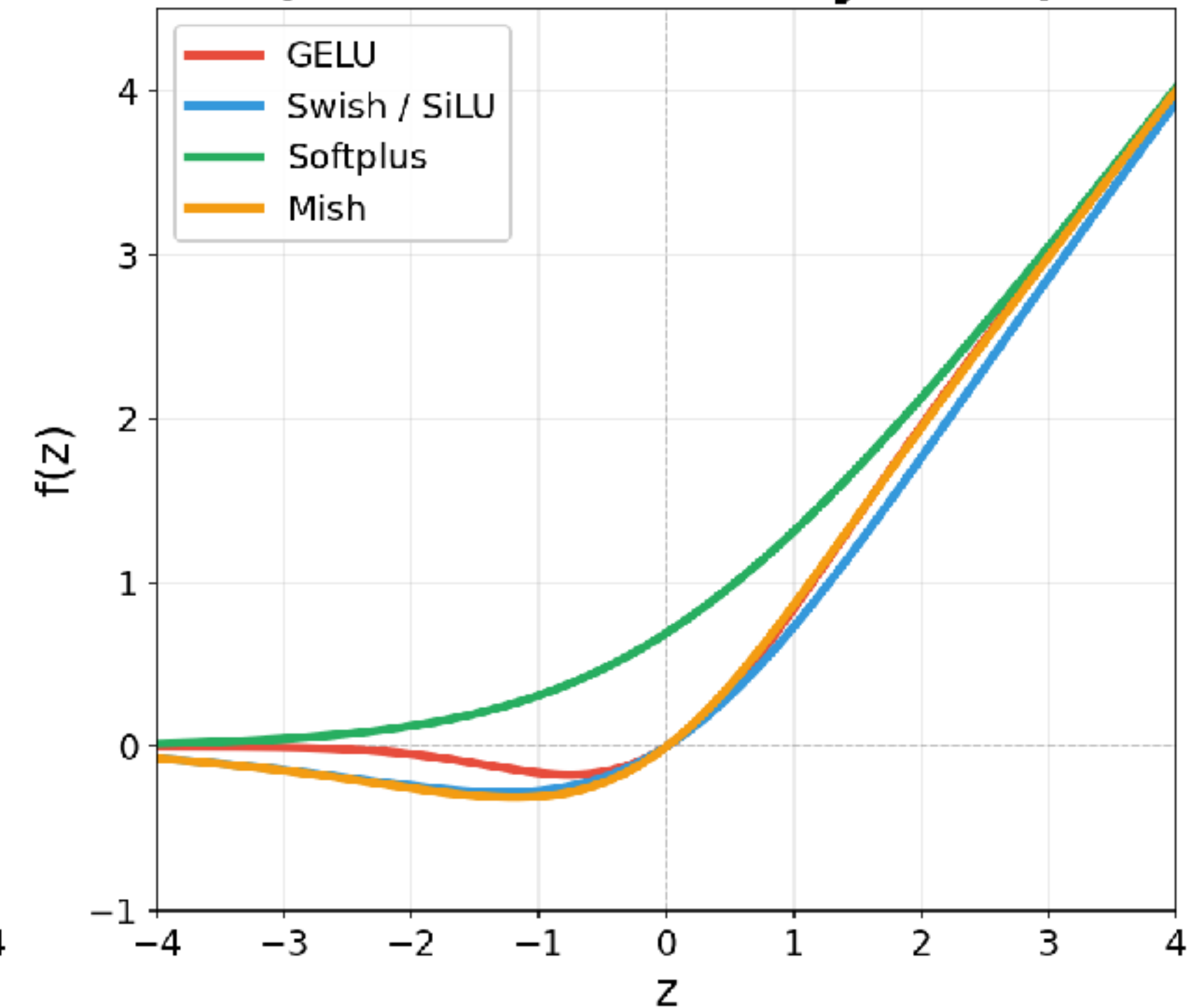
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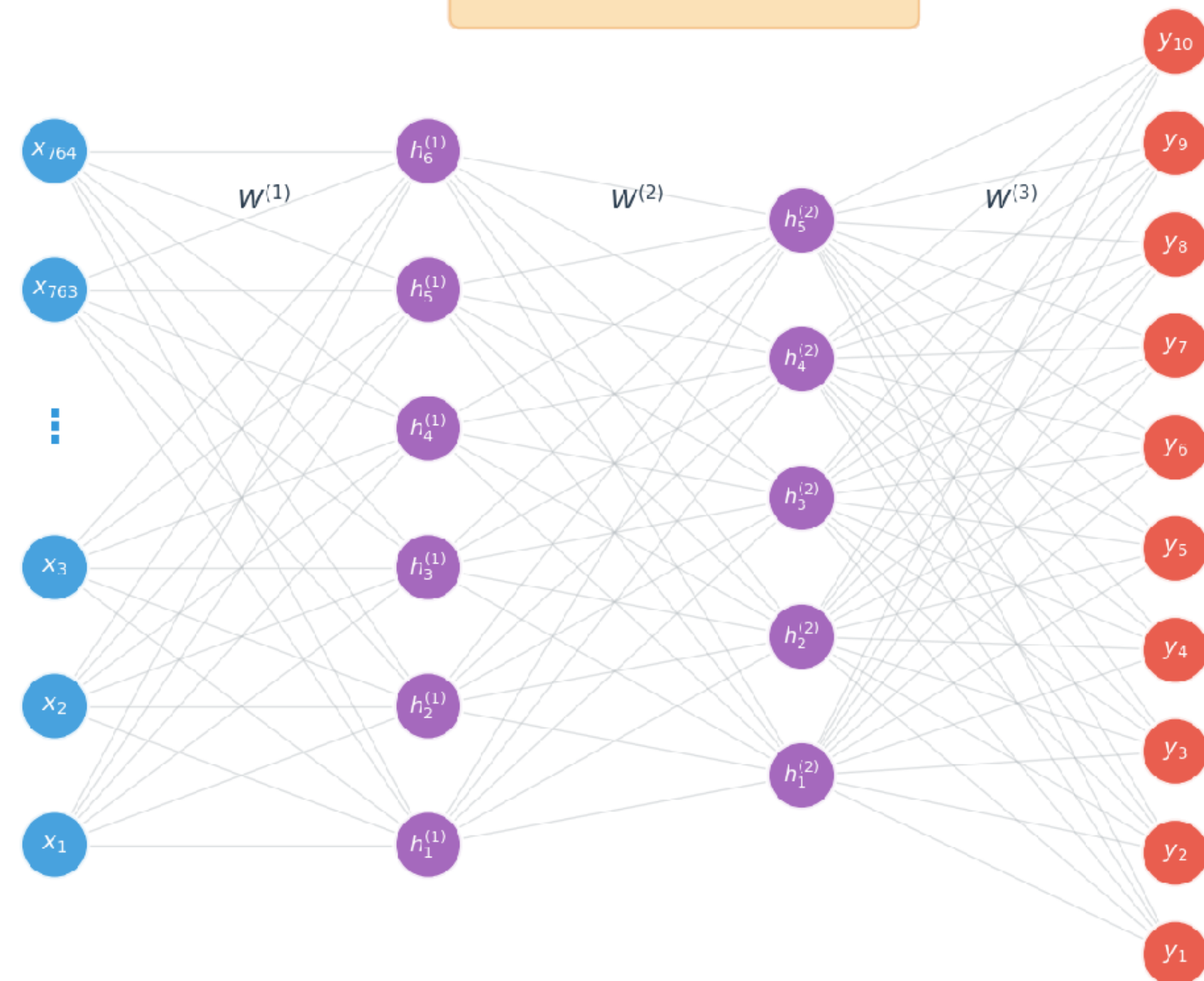


Can you think of “problems” for some of them?

Your First Deep Network!

3-Layer MLP with ReLU Activations

$$\text{ReLU}(z) = \max(0, z)$$



Input Layer
(764 units)

Hidden Layer 1
(ReLU)

Hidden Layer 2
(ReLU)

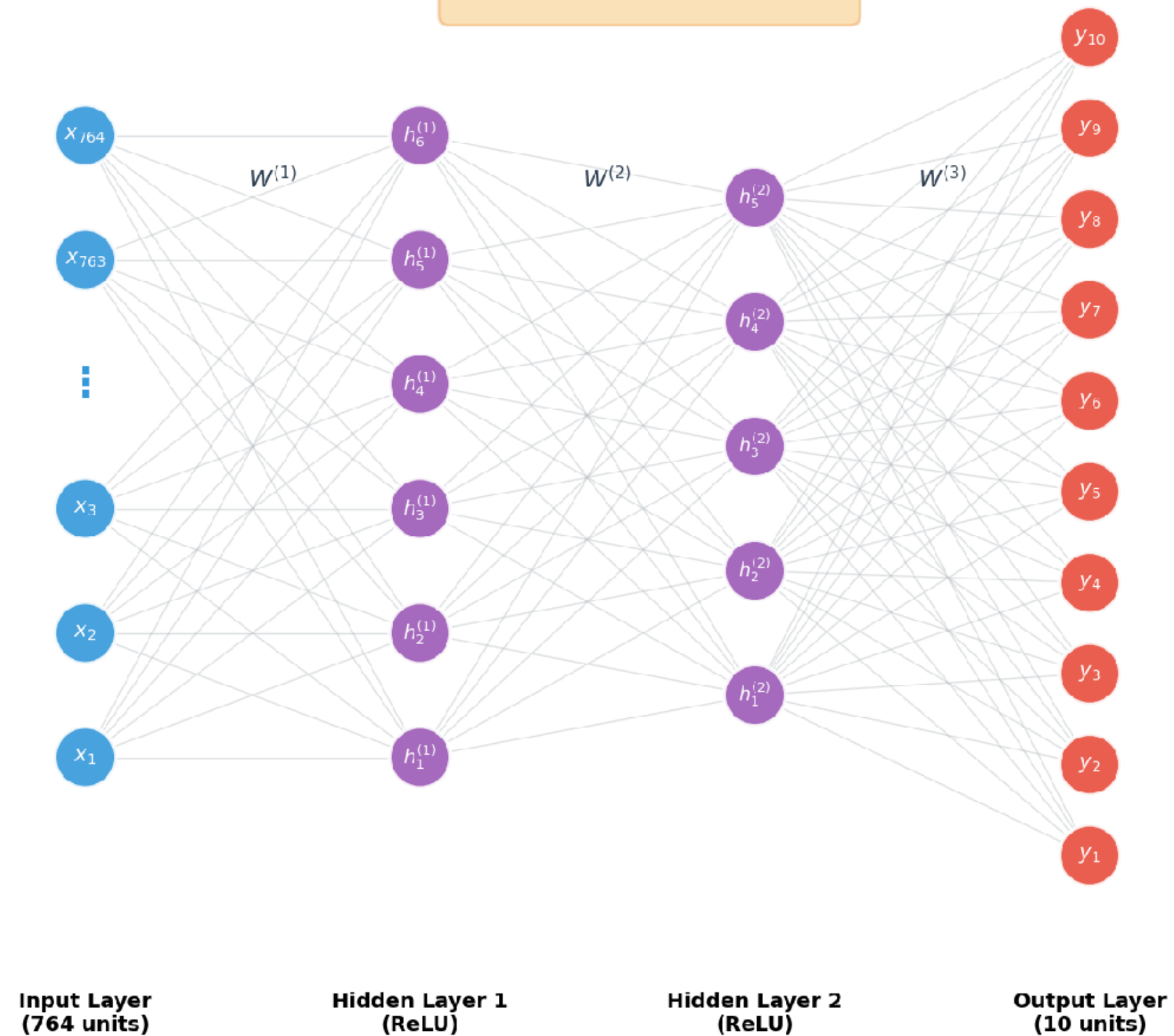
Output Layer
(10 units)

Your First Deep Network!

What training loss?

3-Layer MLP with ReLU Activations

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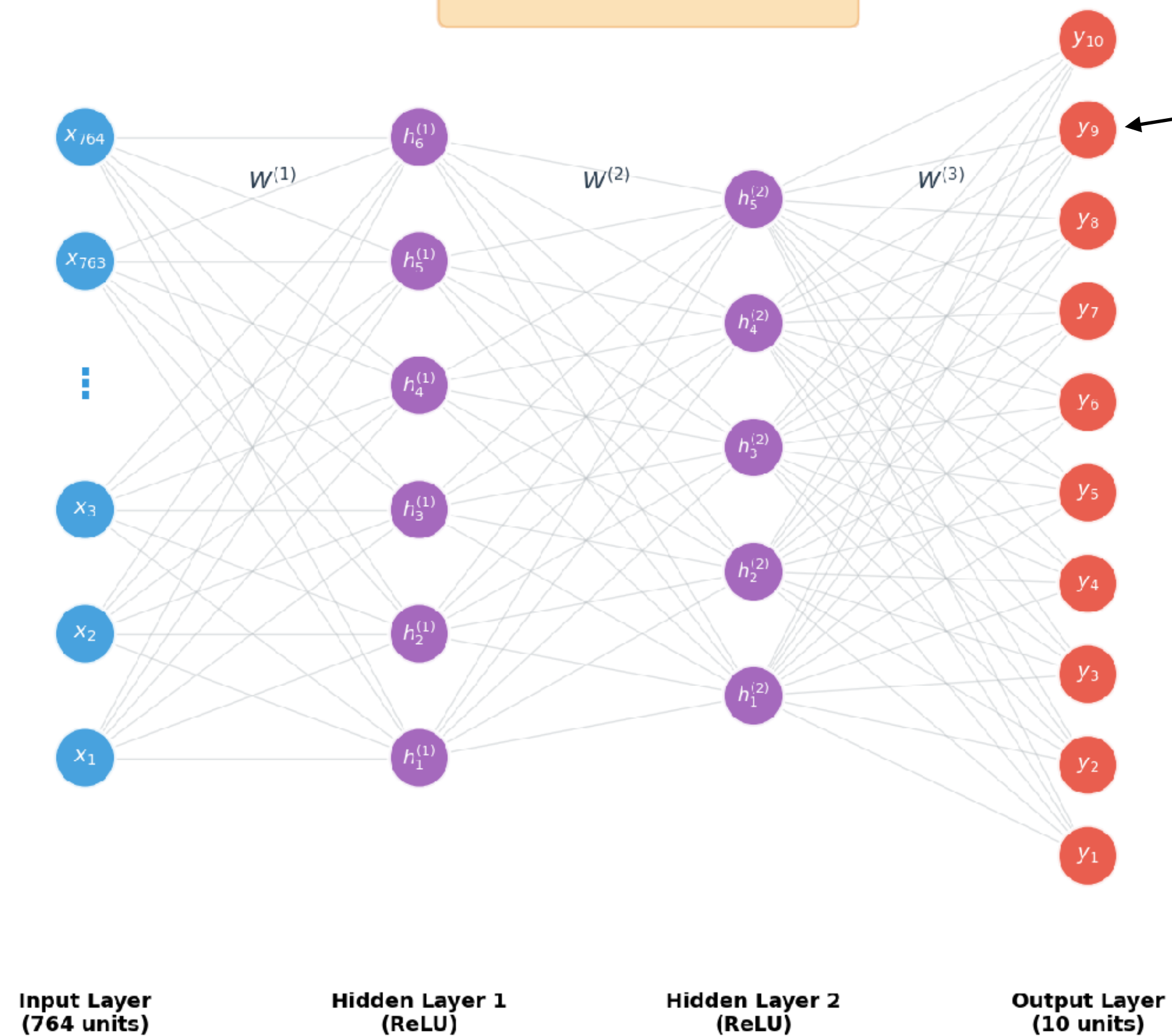


Your First Deep Network!

What training loss?

3-Layer MLP with ReLU Activations

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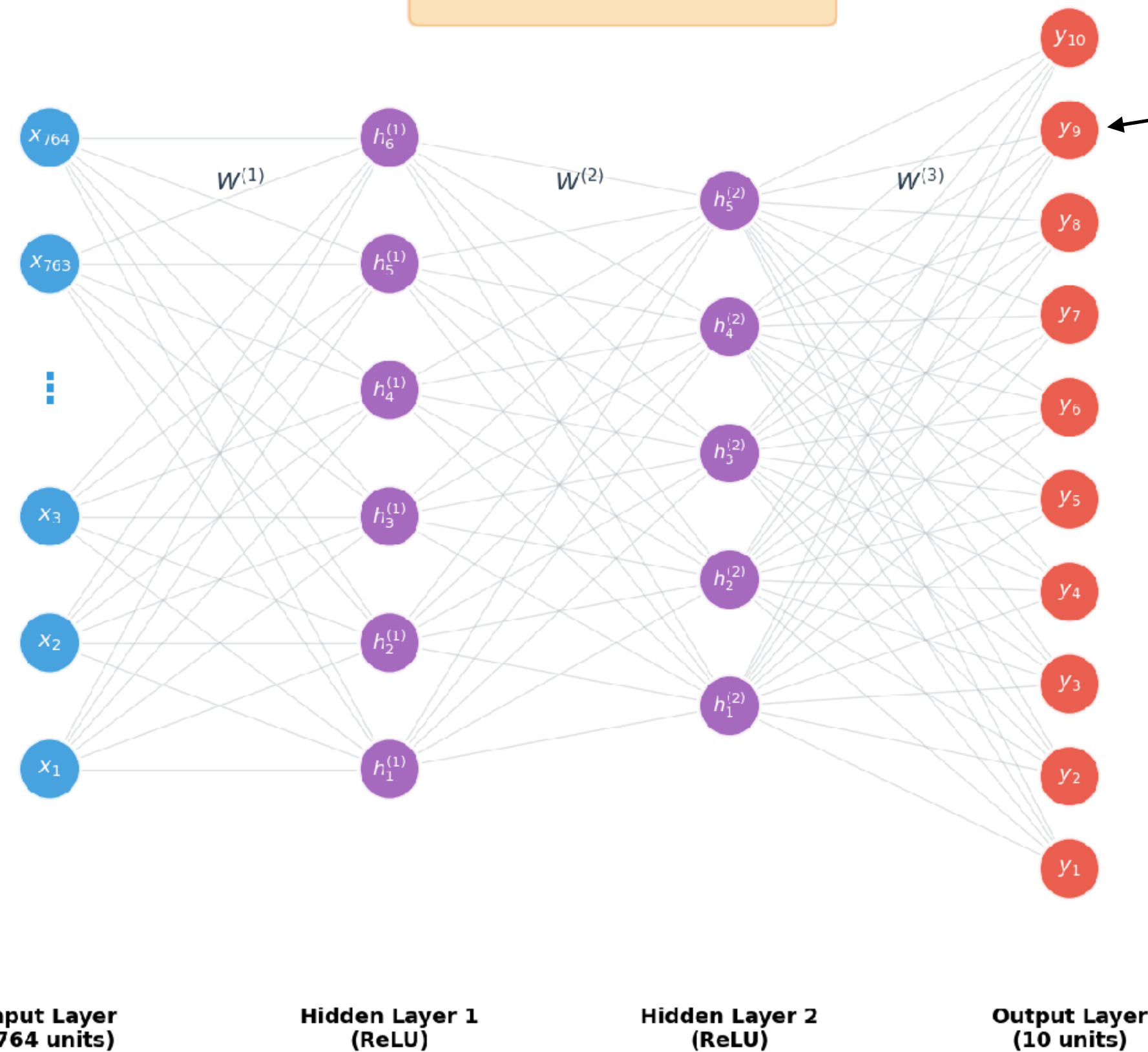
$$p(y = 9 | x_n)$$

Your First Deep Network!

What training loss?

3-Layer MLP with ReLU Activations

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$p(y = 9 | x_n)$

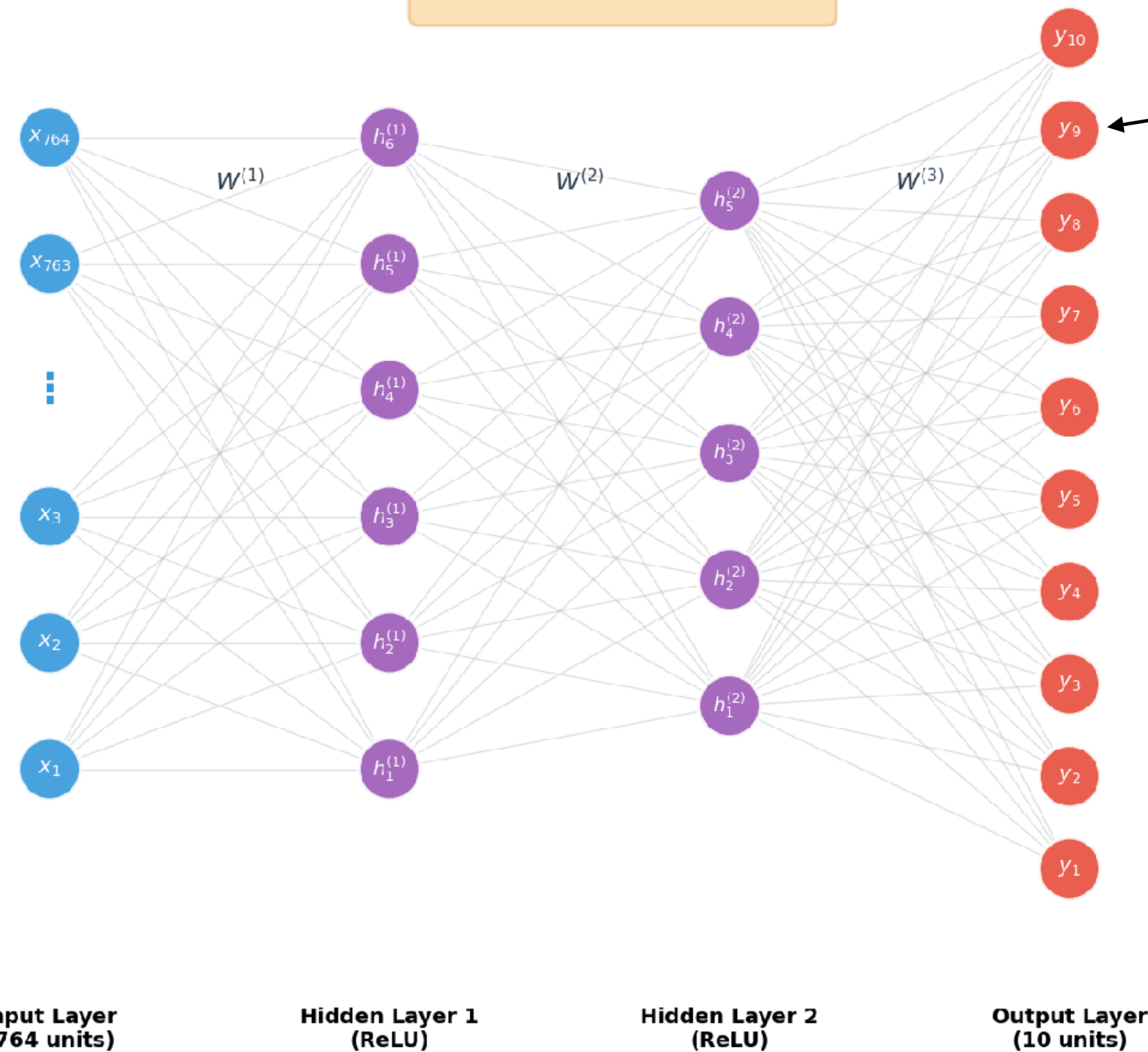
$$\mathcal{L} = - \sum_{n=1}^N \sum_{c=1}^{10} 1_{\{y_n=c\}} \log(p(y = c | x_n))$$

Your First Deep Network!

What training loss?

3-Layer MLP with ReLU Activations

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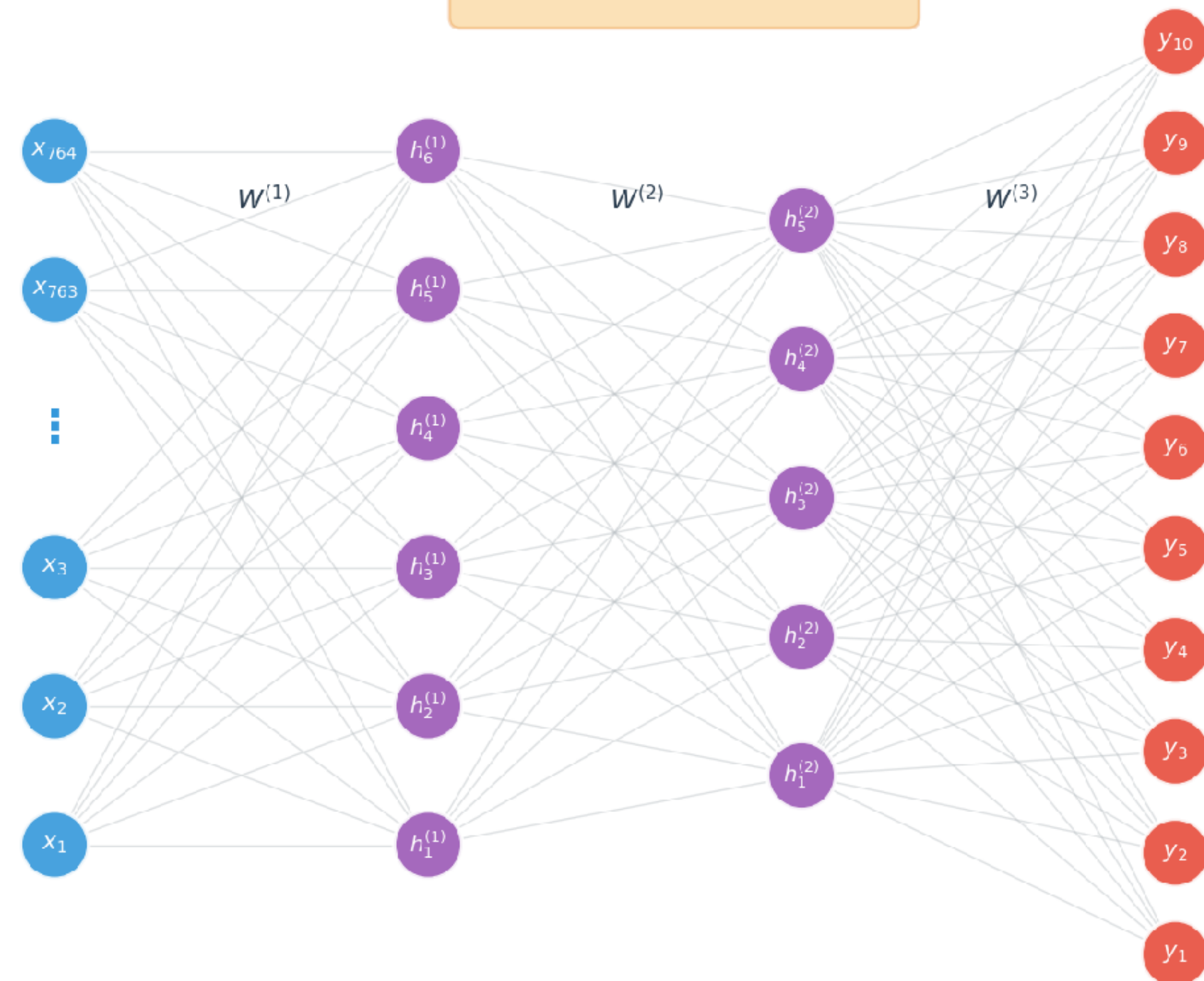
$$\mathcal{L} = - \sum_{n=1}^N \sum_{c=1}^{10} 1_{\{y_n=c\}} \log(p(y = c | x_n))$$

$$\hat{y}_n = \arg \max_{c=1, \dots, 10} p(y = c | x_n)$$

Your First Deep Network: Training

3-Layer MLP with ReLU Activations

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Input Layer
(764 units)

Hidden Layer 1
(ReLU)

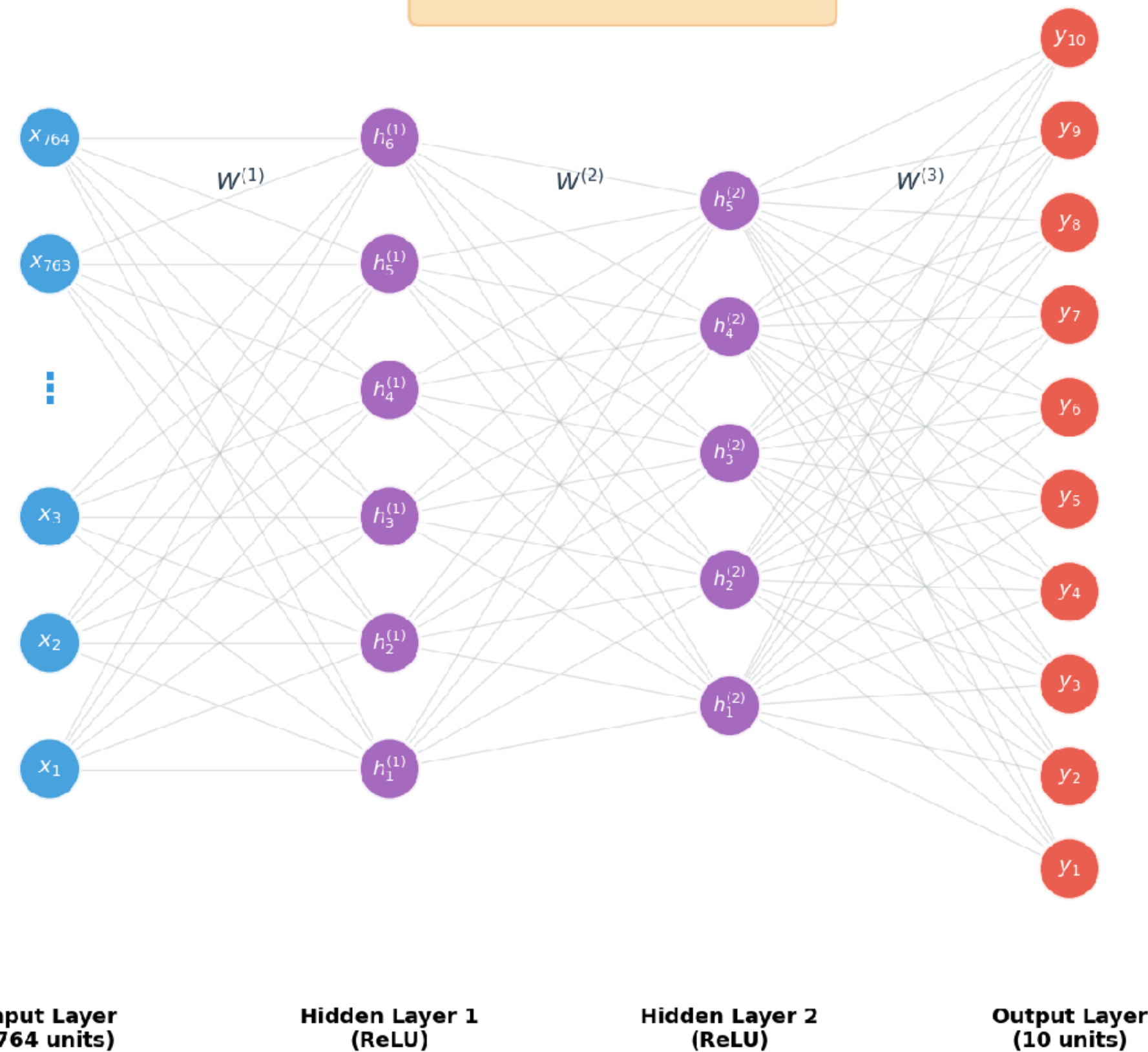
Hidden Layer 2
(ReLU)

Output Layer
(10 units)

Your First Deep Network: Training

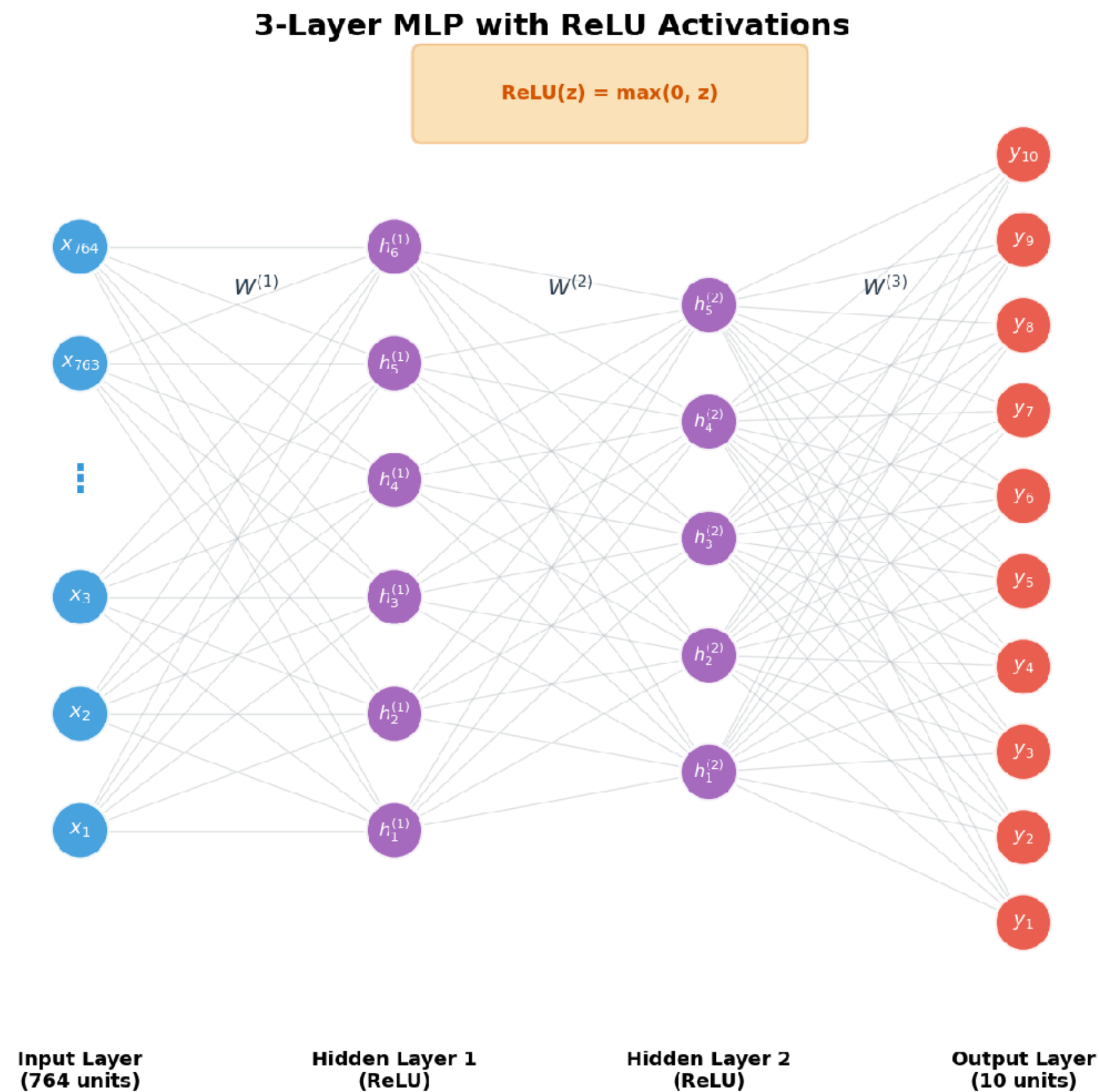
3-Layer MLP with ReLU Activations

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How to train the parameters $W^{(1)}$, $W^{(2)}$, $W^{(3)}$?

Your First Deep Network: Training



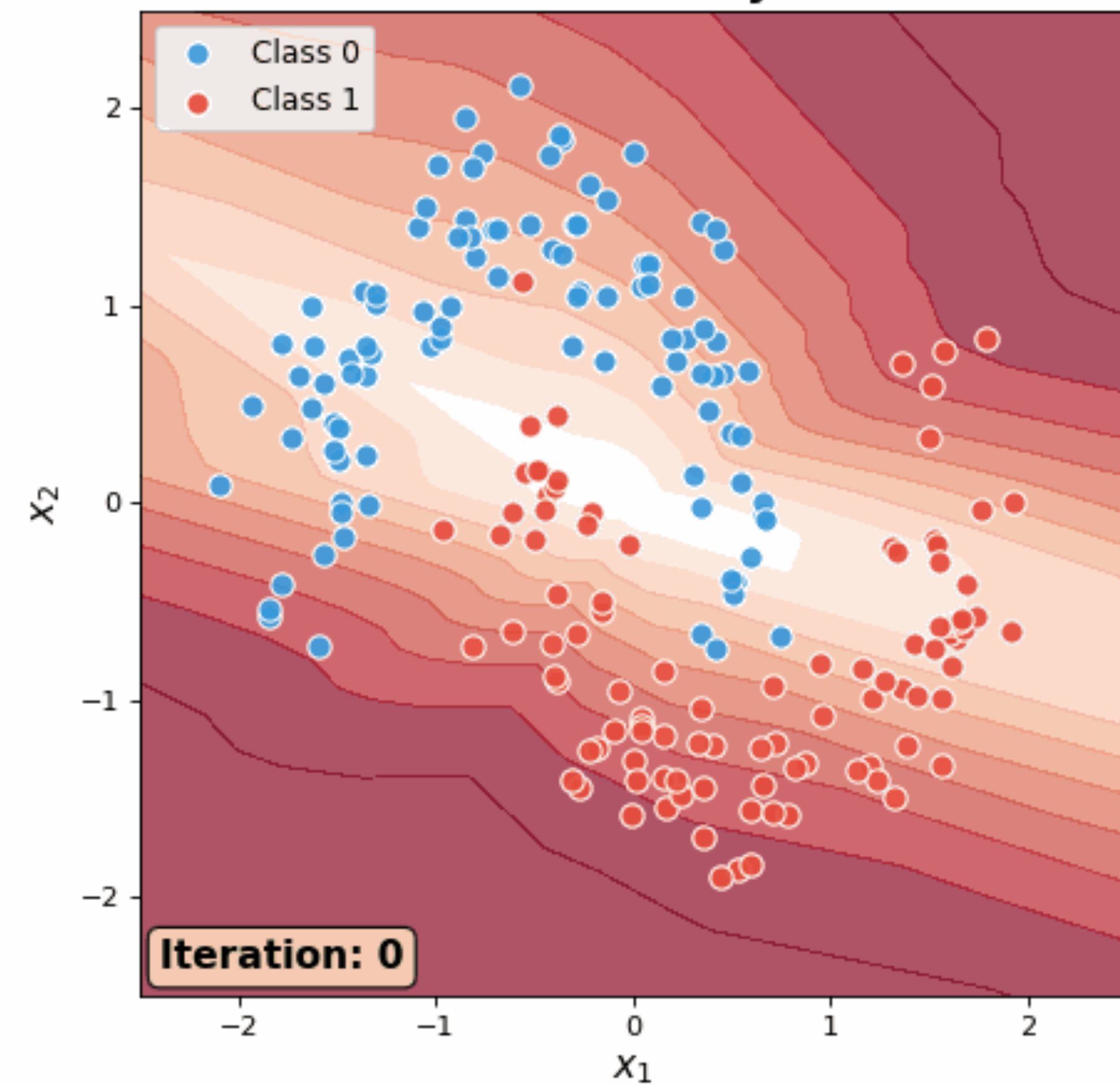
How to train the parameters $W^{(1)}$, $W^{(2)}$, $W^{(3)}$?

Same old gradient descent!

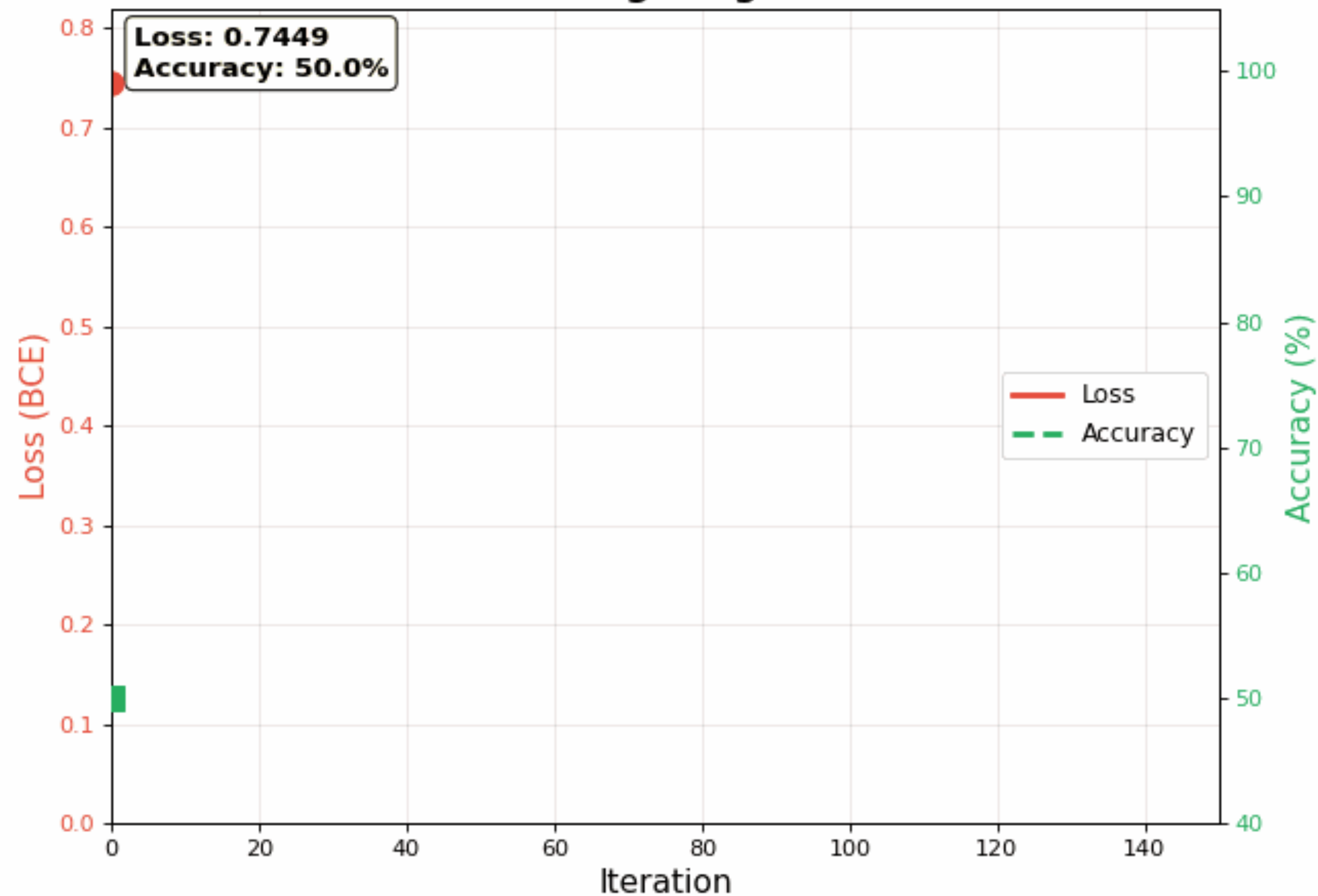
At home: try to derive the gradient
for those 3 matrices

Your First Deep Network: Action!

MLP Decision Boundary (Nonlinear)

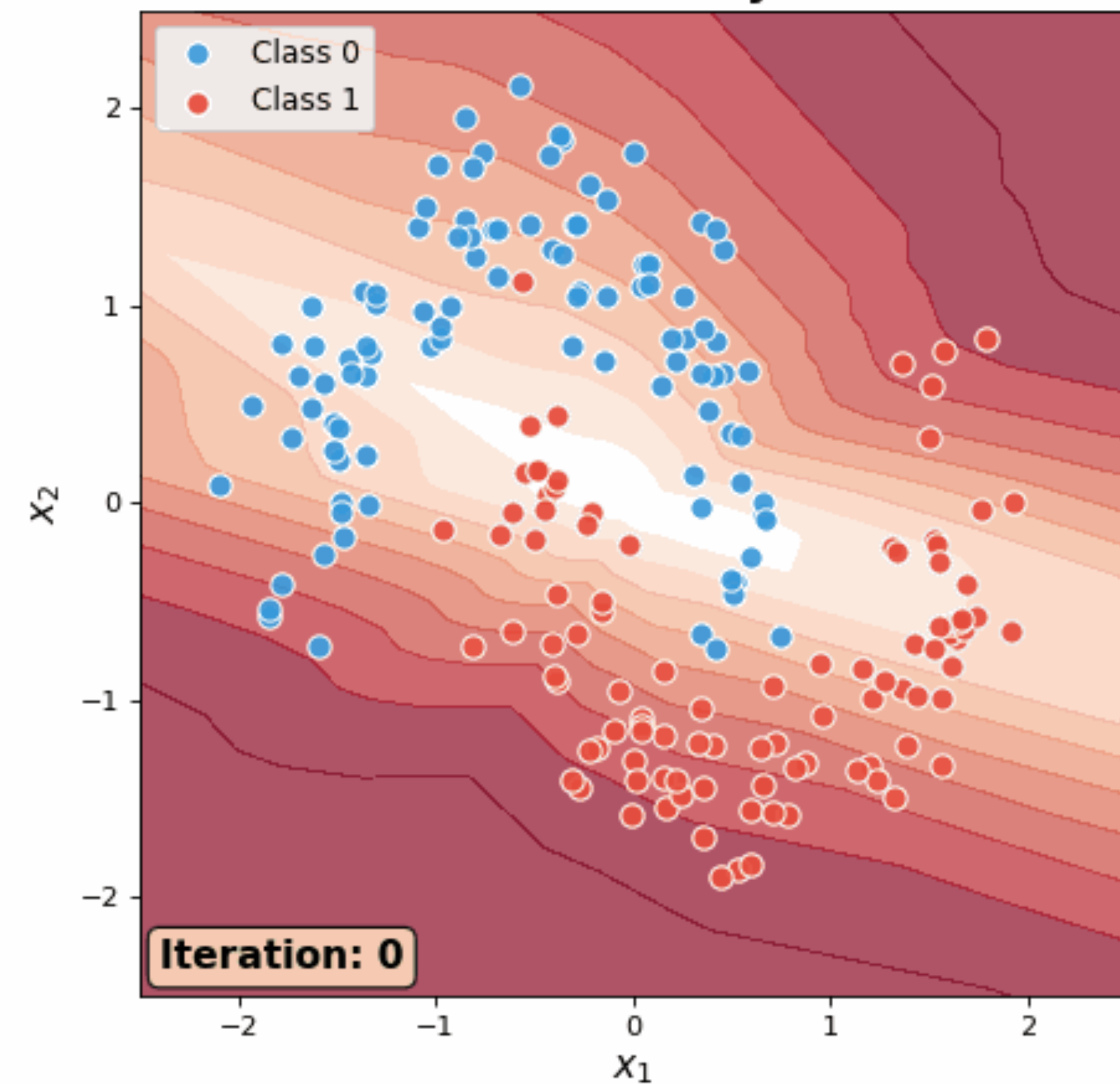


Training Progress

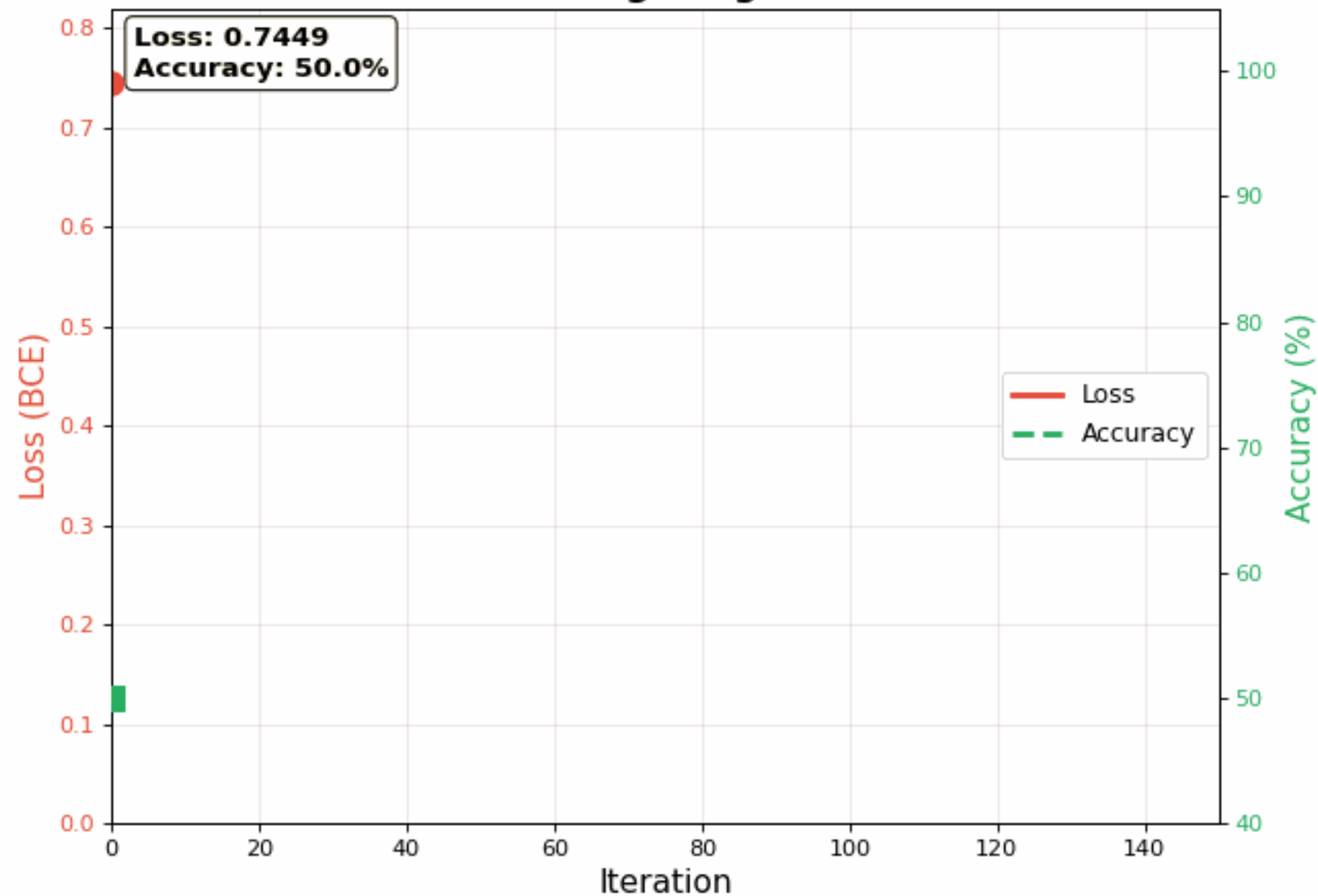


Your First Deep Network: Action!

MLP Decision Boundary (Nonlinear)



Training Progress



Open Discussion

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- Can a Deep Network solve anything?

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- How to search for the right “architecture”?

Open Discussion

- Can a Deep Network solve anything?
- How to search for the right “architecture”?
- How many lines of codes to implement the MNIST model and reach 99.5%?

Questions?